	Test Bo प्रश्नपत्रि Pap PHYSICAI	ooklet (का कोड er-I SC	Code & Ser 5 व क्रमांक [IENCF	ial No.	Α				
G •			Seat No						
Sign	ature and Name of Invigilator		Seat No.						
1. (Si	ignature)		(In figu	res as	in Ao	lmit	Card	l)
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2.(Si	ignature)			(In w	ords)	•••••	•••••	•••••	••••
(N	ame)	MR S	heet No.						
MA	AB - 32223			(To be	filled	 bv th	l e Ca	l ndid	L ate)
Tim	e Allowed : 2 Hours]			1000	Maxir	num	Ma	rks :	200
Num	ber of Pages in this Booklet : 24	Nı	umber of	Questi	ons in	this	Bool	slet :	$\frac{-00}{100}$
	Instructions for the Candidates			विद्यार्थ्यांसा	ठी महत्त्वाच	व्या सच	ना		
1.	Write your Seat No. and OMR Sheet No. in the space provided	1.	परीक्षार्थींनी आ	पला आसन	क्रमांक या प्	गुष्ठावरील गुष्ठावरील	1 वरच्या	कोपऱ्यात	1 लिहावा
2.	This paper consists of 100 objective type questions. Each question		तसेच आपणांस	न दिलेल्या उ रोज 100 ज	तरपत्रिकेचा नगर्गाणे गण	क्रमांक ज आहेत	त्याखाली प्राच्चेन	। लिहावा गणनाम	- के न नग
3.	will carry <i>two</i> marks. <i>All</i> questions of Paper II will be compulsory. At the commencement of examination, the question booklet	2.	संदर प्रश्नपात्र आहेत. या प्रश	कत 100 ब नपत्रिकेतील	हुपयाया प्रश् सर्व प्रश्न स	न आहत गेडविणे	• प्रत्यक अनिवार्य	प्रश्नास राआहे.	દાન ગુળ
	will be given to the student. In the first 5 minutes, you are	3.	परीक्षा सुरू झ	ाल्यावर विद्य	ार्थ्याला प्रश	नपत्रिका	दिली ज	ाईल. सुर	ल्वाती च्या
	requested to open the booklet and compulsorily examine it as follows :		5 मिनिटांमध्ये	आपण सद	र प्रश्नपत्रि	का उघड़	रून खाल	ील बार्ब	ो अवश्य
	(i) To have access to the Question Booklet, tear off the		तपासून पहाव्य	ात.					
	paper seal on the edge of this cover page. Do not accept		(i) प्रश्न ¹	गत्रिका उघड	ण्यासाठी प्रश	नपत्रिके	वर लावल	लेले सील	उघडावे.
	(<i>ii</i>) Tally the number of pages and number of questions in		साल	नसलला ाक	वा साल उध	त्रडलला	प्रश्नपात्र	का स्वाव	कारू नय. चर्म
	the booklet with the information printed on the cover		(u) पाहल नापेन	या पृष्ठावर पाण्डागनिको	नमूद कल्प नीच प्रकार	॥प्रमाण मण्डां= ी	प्रश्नपात्र	कचा एव गटनान	कूण पृष्ट र गटानी
	page. Faulty booklets due to missing pages/questions or questions repeated or not in serial order or any		तस्य प्राप्ते	्ररूप पात्रक कमी अमले	ताल एकूण जी/कमी मा	प्रशाम जन्भूमल	। सख्या केली/प्रप	पडताळू गंचा चत	1 पहापाः तीचा का
	other discrepancy should not be accepted and correct		रूप रामन	केली किंवा द	ता/ फना अप नर चटी अम्ब	लेली सद	ोष प्रश्नेष	ापा पुप जिका स	ग पा अग्न हवातीच्य
	booklet should be obtained from the invigilator within		5 मि	निटातच पर्यव	तेर नुडा जात बेक्षकाला प	लला अप रत देऊन	दसरी प्र	गत्रपत्रिक श्नपत्रिक	रजाता ज्य त मागवन
	Booklet will be replaced nor any extra time will be		घ्यार्व	ो. त्यानंतर प्र	। इनपत्रिका	बदलन वि	्रुः मळणार :	नाही तसे	च वेळही
	given. The same may please be noted.		বাটক	न मिळणार र	नाही याची व	रुपया वि	द्यार्थ्यांनी	नोंद घ्या	वी.
	(<i>iii</i>) After this verification is over, the OMR Sheet Number		(iii) वरील	नेप्रमाणे सब	र्ग पडताळू	- न पाहिल	त्यानंतरन	व प्रश्नग	गत्रिकेवर
4.	Each question has four alternative responses marked (A), (B).		ओ.ए	म.आर. उत्तर	पत्रिकेचा ने	बर लिहा	वा.		
	(C) and (D). You have to darken the circle as indicated below on	4.	प्रत्येक प्रश्नास	ia (A), (B)	, (C) आणि	(D) अश	गी चार वि	वेकल्प उ	जत्तरे दिर्ल
	the correct response against each item. Example : where (C) is the correct response		आहेत. त्यातीत	त योग्य उत्त	राचा रकाना	खाली	दर्शविल्य	गप्रमाणे	ठळकपण्
			কাळা/নিळা ক	रावा					
			उदा. : जर (C) ह याग्य उत्त	ार असल त	τ.	\sim		
5.	Your responses to the items are to be indicated in the OMR			(A)	(в) ((D)		
	Sheet given inside the Booklet only. If you mark at any place other than in the circle in the OMR Sheet it will not be evaluated	5.	या प्रश्नपत्रिकेल	गील प्रश्नांची	उत्तरे ओ.एग		् उत्तरपत्रिक	केतच दः	र्शवावीत
6.	Read instructions given inside carefully.		इतर ठिकाणी लि	नहिलेली उत्तरे	तपासली जा	णार नाहीत	Ŧ.		
7.	Rough Work is to be done at the end of this booklet.	6.	आत दिलेल्या	सूचना काळज	जीपूर्वक वाच	त्राव्यात.			
8.	If you write your Name, Seat Number, Phone Number or put	7.	प्रश्नपत्रिकेच्या	शेवटी जोड	लेल्या को-य	॥ पानावर	त्व कच्चे	। काम क	रावे.
	any mark on any part of the OMR Sheet, except for the space	8.	जर आपण ओ	.एम.आर. व	र नमूद केले	ोल्या ठिव	काणाव्यकि	तेरिक्त इत	ार कोठेही
	identity, or use abusive language or employ any other unfair		नाव, आसन ब्र	ज्मांक, फोन	नंबर किंवा	ओळख	पटेल अ	शी कोणल	तीही खूण
	means, you will render yourself liable to disqualification.		केलेली आढळू	न आल्यास ३	नथवा असभ्य	य भाषेचा	वापर कि	वा इतर ग	गैरमागांच
9.	You have to return original OMR Sheet to the invigilator at the		अवलब कल्य	सं विद्यार्थ्या	ला परक्षिस	अपात्र ठ	रविण्यात	यईल.	
	end of the examination compulsorily and must not carry it with	9.	पराक्षा सपल्याः	नतर विद्यार्थ्य	।न मूळ ऑ. ¹ जणपि ज्यान	्म-आर.	उत्तरपात्र को नग	।का पयव ००० -	क्षकाकड संकाकड
	to carry the Test Booklet and duplicate conv of OMR Sheet on		परत करण आव विनीय एव २०००	१२४१क आह. प्रत्यालगोला	तथा। ५, प्रश्न नेप्राप्त जिन्द	भात्रका व _{गर्थ्या} न	आः एमः मना गरी	आरः उत्तर आटे	(पात्रकच
	conclusion of examination.	10	ाह्रताथ प्रत आ रहन जिल्ला कि	भएपाबराबर कंता कार्यका	नण्यास ।वर्ध बॉल गेवन्ग	미~에 데 년 '파 제'''''	1रवानगा क्याला	আছ.	
10.	Use only Blue/Black Ball point pen.	10.	ਆ ਗ । ¶ळ्या । कॅलक्सकेंटर कि	न पा फाळ्या केवा लॉग रेग	आल पनच बल ताण्णण्	ज जापर एस एएटर	कराषाः नगी नार्ट	Ĵ.	
11.	Use of any calculator or log table, etc., is prohibited.	11.	जलानपुरादर । चकीच्या उत्तम	न्यता साम टर स्माती गण व्य	नरा जानरण्ड त्यात केली व	तत्व १९२१ जाणार सा	ात्मा ताल ही.		
12.	There is no negative marking for incorrect answers.	12.	ગુવત બ્લા ઉપાર	ાંગ મુંગ પ	ave avents	-a -uX -H	Q1.		

Physical Science Paper II

Time Allowed : 120 Minutes] [Maximum Marks : 200

Note : This Paper contains Hundred (100) multiple choice questions. Each question carrying Two (2) marks. Attempt *All* questions.

1.	Which of the following is an analytic	4.	A function $f(x)$ satisfies th differential equation	e n
	function ?		$\frac{d^2f}{dx^2} - \omega^2 f(x) = -\delta(x-a)$, where ω is	s
	(A) $z \pm \overline{z}$ (B) z^2		positive. The Fourier transform	n
			$F(k) = \int_{-\infty}^{\infty} f(x)e^{ikx}dx$ and solution	n
	(C) $z\overline{z}$ (D) z/\overline{z}		f(x) of the differential equations ar respectively :	e
2.	Which of the following statements			
	is true ?		(A) $\frac{e^{ika}}{k^2 - \omega^2}$ an	d
	(A) Trace (AB) = Trace (BA)		$\frac{1}{2\omega} \big(e^{-i\omega x-a } + e^{i\omega x-a } \big)$	
	(B) Trace (ABC) = Trace (BAC)		$(\mathbf{P}) e^{ika}$	1
	(C) Trace (ABCD) = Trace (BACD)		(B) $\frac{1}{k^2 - \omega^2}$ and $\frac{1}{k^2 - \omega^2} \left(\frac{1}{2} \frac{1}{2}$	a
	(D) Trace (AB) = Trace (A) Trace (B)		$\frac{1}{2i\omega} \left(e^{-i\omega i\omega - \omega + \frac{1}{2}} e^{i\omega i\omega - \omega + \frac{1}{2}} \right)$	
3.	Laplace transform $F(s)$ of a function		(C) $\frac{e^{ika}}{k^2 + \omega^2}$ an	d
	$f(x) = 1$, for $0 \le x \le \infty$ is equal to:		$rac{1}{2\omega}ig(e^{-\omega x-a }+e^{\omega x-a }ig)$	
	(A) 1/s (B) 1/s ²			
	(C) <i>s</i> (D) 2 <i>s</i>		(D) $\frac{e^{ika}}{k^2 + \omega^2}$ and $\frac{1}{2\omega}e^{-\omega x-a }$	

5. The integral

$$\frac{1}{2\pi i} \oint \frac{\exp\left[\frac{z}{2}\left(t-\frac{1}{t}\right)\right]}{t^{n+1}} dt,$$

where n is an integer and the closed contour is a circle enclosing the origin, can be used to :

- (A) generate Hermite polynomials
- (B) generate Bessel's functions of first kind
- (C) generate Legendre polynomials
- (D) generate associated Legendre polynomials

6. The value of
$$\oint z \exp\left(\frac{1}{z}\right) dz$$
, where
the closed contour is a unit circle

traversed anticlockwise is :

- (A) πi (B) $2\pi i$ (C) π (D) 0
- 7. Consider vectors \$\vec{a} = \holdsymbol{\hat{i}} + 5\holdsymbol{\hat{j}} + \holdsymbol{k}\$,
 \$\vec{b} = \holdsymbol{\hat{i}} 5\holdsymbol{\hat{j}} + \holdsymbol{k}\$ and \$\vec{c} = \holdsymbol{\hat{i}} + \holdsymbol{k}\$. Which of the following statements is true ?
 (A) \$\vec{a}\$, \$\vec{b}\$, \$\vec{c}\$ are linearly independent
 (B) \$\vec{a}\$, \$\vec{b}\$, \$\vec{c}\$ are linearly dependent
 (C) \$\vec{a}\$, \$\vec{b}\$, \$\vec{c}\$ are orthogonal
 (D) \$\vec{a}\$, \$\vec{b}\$, \$\vec{c}\$ are normalized

8. Consider the following probability density function :

$$P(x) = 0 \ x < -2 \ \text{and} \ x > 3$$

$$P(x) = a \ -2 < x < 2$$

$$P(x) = \frac{1}{12} \ 2 < x < 3$$
The value of *a* is :

(A)
$$\frac{11}{12}$$
 (B) $\frac{1}{12}$
(C) $\frac{11}{48}$ (D) $\frac{1}{48}$

9. The Green's function $G(x, x_0)$ satisfying the equation

$$\frac{d^{2}\mathrm{G}(x,x_{0})}{dx^{2}} = \delta(x-x_{0})$$

with boundary conditions $G(-L, x_0) = G(L, x_0) = 0$ is :

(A)
$$\begin{cases} \frac{1}{2L} (L - x_0) (x + L) - L \le x \le x_0 \\ \frac{1}{2L} (x_0 + L) (L - x) x_0 \le x \le L \end{cases}$$

(B)
$$\begin{cases} \frac{1}{2L} (x_0 + L) (x + L) - L \le x \le x_0 \\ \frac{1}{2L} (x_0 - L) (x - L) x_0 \le x \le L \end{cases}$$

(C)
$$\frac{1}{2L}(x-L)(x+L)-L \le x \le L$$

(D)
$$\begin{cases} \frac{1}{2L} (x_0 - L) (x + L) - L \le x \le x_0 \\ \frac{1}{2L} (x_0 + L) (x - L) x_0 \le x \le L \end{cases}$$

10. Two students solved the Poisson's

equation $\nabla^2 \varphi = -\frac{\rho_0}{\varepsilon_0}$ (the symbols have usual meanings). They obtained two different answers $\varphi_1(x) = -\frac{1}{2} \frac{\rho_0 x^2}{\varepsilon_0}$

and $\varphi_2(y) = -\frac{1}{2} \frac{\rho_0 y^2}{\varepsilon_0}$. What is the reason?

- (A) Space is isotropic, hence x andy are equivalent
- (B) We can add solution of Laplace's equation to both
- (C) The boundary conditions are different in the two cases
- (D) One of them was wrong
- 11. The equation $\tan (2x) = x^2 4$ has :
 - (A) One real root
 - (B) Two real roots
 - (C) No real root
 - (D) Infinitely many real roots

- 12. The order of magnitude of the error in estimating the value of integral $\int_0^{10} (5x+6) dx$ numerically using trapezoidal method with a step size of 0.1 is : (A) 0 (B) 10^{-2}
- (C) 10⁻³
 (D) 10⁻¹
 13. The deflection of a structure under loading is measured at five different values of the force applied X in kilo Newtons (kN). The deflection Y is in centimetres. Data are given in the following table. Employing
 - following table. Employing Lagrange's interpolation with quadratic polynomial, compute the extrapolated value of the deflection Y for zero load (X = 0 kN). How many points are used ?

X (kN)	0.5	1.0	1.5	2.0	2.5
Y (cm)	3.0	3.9	5.2	7.3	10.5
(A) 4.05	5, 2		(B)	2.5	0, 3
(C) 2.00), 4		(D)	2.0	0, 5

- 14. Which of the following equations represents a conservative force ?
 - (A) $\overline{\mathbf{F}} = (xy + z^2)\hat{i} + x^2\hat{j} 2xz\hat{k}$
 - (B) $\overline{\mathbf{F}} = (2xy + z^2)\hat{i} + x^2\hat{j} + 2xz\hat{k}$
 - (C) $\overline{\mathbf{F}} = (xy z^2)\hat{i} x^2\hat{j} + 2xz\hat{k}$
 - (D) $\overline{\mathbf{F}} = (xy z^2)\hat{i} + x^2\hat{j} + 2xz\hat{k}$

5

15. For a particle moving under the action of a central force, the correct relation between the energy (E) of the particle, eccentricity (e) of the conic section describing the orbit, reduced mass (μ), angular momentum (\overline{l}), and the force constant (k) is given by :

(A)
$$\mathbf{E} = \frac{\mu k^2}{2l^2} (e^2 - 1)$$

(B) $\mathbf{E} = \frac{\mu k^2}{l^2} (1 - e^2)$
(C) $\mathbf{E} = \frac{\mu k^2}{l^2} (1 + e^2)$
(D) $\mathbf{E} = \frac{\mu k^2}{2l^2} (e^2 + 1)$

- 16. Consider two frames XYZ and xyzhaving common origin. The frame XYZ is fixed and the frame xyz is rotating with angular velocity (ω) with respect to the frame XYZ. Here $\overline{\omega} = 2t\hat{x} - 5t^2\hat{z}$, where t represents time. For a given position vector (\overline{r}) defined as $\overline{r} = 4t^2\hat{x} + 6t\hat{y} + t^3\hat{z}$ in the xyz coordinate frame, the velocities in frames XYZ and xyz for t = 1, will be respectively : (A) $8\hat{x} - 6\hat{y} + 3\hat{z}$ and $38\hat{x} + 16\hat{y} + 15\hat{z}$
 - (B) $38\hat{x} 16\hat{y} + 15\hat{z}$ and $8\hat{x} + 6\hat{y} + 3\hat{z}$
 - (C) $8\hat{x} + 6\hat{y} + 3\hat{z}$ and $38\hat{x} 16\hat{y} + 15\hat{z}$
 - (D) $38\hat{x} + 16\hat{y} + 15\hat{z}$ and $8\hat{x} 6\hat{y} + 3\hat{z}$

17. A circular platform is rotating with uniform angular speed ω counterclockwise about an axis passing through its center and perpendicular to its plane (as shown in figure). A person of mass *m* walks radially inwards with a uniform speed *v* on the platform. The magnitude and direction of the Coriolis force (with respect to the direction along which the person walks) is :



- (A) $mv\omega$ towards his right
- (B) $2mv\omega$ towards his right
- (C) $mv\omega$ towards his left
- (D) $2mv\omega$ towards his left

18. Consider an inverted pendulum comprised of a mass m attached to a rigid massless rod of length l as shown in figure. The point 'O' exhibits vertical motion (along z direction) described by equation $z = a \sin\omega t$, where ω is constant. The Lagrangian of the system is given as :



19. A mass spring system consists of two blocks of mass M and one block of mass m (<M). The blocks are connected with two springs of same spring constant (k), as shown in figure. The system is constraint to move along a straight line on a frictionless horizontal surface. Let V represent the potential energy of the system. Considering that the masses are exhibiting small oscillations, the potential energy matrix (V) is given as :

	k M_₩	√ m	- ₩₩ [M]
(A)	$rac{1}{2}igg(egin{array}{c}k\\-k\\0\end{array}igg)$	-k $2k$ $-k$	$egin{array}{c} 0 \ -k \ k \end{array} ight)$	
(B)	$rac{1}{2}igg(egin{array}{c}k\\0\\-k\end{array}igg)$	$0 \\ 2k \\ k$	$egin{array}{c} -k \ k \ 0 \end{array} ight)$	
(C)	$rac{1}{2}inom{k}{k}{0}$	-k $2k$ k	$\begin{pmatrix} 0\\k\\k \end{pmatrix}$	
(D)	$rac{1}{2}igg(egin{array}{c} -k \ 0 \ k \ \end{array}igg)$	0 2k k	$egin{array}{c} k \ -k \ k \end{array} ight)$	

- 20. Consider two persons A and B of same age, 20 years. Person A remains rest at origin, whereas person B takes a roundtrip space voyage to a star with velocity v = 0.99c relative to person A (where c is the speed of light). The round trip distance travelled by the person B is 20 light years. When B meets A after completion of the space voyage, their ages are :
 - (A) A : 40.2 yrs, B : 40.2 yrs
 - (B) A : 40.2 yrs, B : 22.8 yrs
 - (C) A : 22.8 yrs, B : 22.8 yrs
 - (D) A : 40.8 yrs, B : 40.2 yrs
- 21. The number of degrees of freedom describing motion of a swimmer in a swimming pool is :
 - (A) 3 (B) 5
 - (C) 6 (D) 9
- 22. For a conservative dynamical system, the area enclosed by the phase space :
 - (A) Increases with time
 - (B) Remains constant with time
 - (C) Decreases with time
 - (D) Oscillates with time

- 23. Hamilton's principal function S and Hamilton's characteristic function W for a conservative system, are related as :
 - (A) $S(q_k, t) = W(q_k) E$ (B) $S(q_k, t) = W(q_k) + E$ (C) $S(q_k, t) = W(q_k) + Et$ (D) $S(q_k, t) = W(q_k) - Et$
- 24. For a particle moving in an inverse square force field, $V(r) = -\frac{K}{r}$, the action angle variable analysis gives :
 - (A) only one frequency of oscillation
 - (B) two similar frequencies of oscillation
 - (C) two dissimilar frequencies of oscillation
 - (D) more than two dissimilar frequencies of oscillation
- 25. If J is the current density and ρ is the electric charge density, then

equation $\vec{\nabla} \cdot \vec{j} + \frac{\partial \rho}{\partial t} = 0$ represents :

- (A) wave equation
- (B) continuity equation
- (C) Poisson's equation
- (D) Laplace's equation

- 26. If the potential function is a step function, the relevant equation is :
 - (A) Laplace's equation
 - (B) Poisson's equation
 - (C) Maxwell's equation
 - (D) Ampere's equation
- 27. An electric field applied along the length of a long circular cylinder produces a polarization P. The depolarization field produced in this configuration is :
 - (A) $4\pi P / 3$ (B) $-4\pi P / 3$

(C) $2\pi P$ (D) 0

- 28. The electric field of an electromagnetic wave is $\vec{E} = i\sqrt{2} \sin(kz \omega t)$ V/m. The average flow energy per unit area per unit time, due to this wave is :
 - (A) $27 \times 10^4 \text{ W/m}^2$ (B) $27 \times 10^{-4} \text{ W/m}^2$ (C) $27 \times 10^{-2} \text{ W/m}^2$ (D) $27 \times 10^2 \text{ W/m}^2$

- 29. When a monoatomic gas atom is placed in a uniform electric field, the resulting induced dipole moment is :
 - (A) proportional to E
 - (B) proportional to E^2
 - (C) proportional to E^3
 - (D) independent of E
- 30. The reflection coefficient k_r , characteristic impedance Z_0 , and load impedance Z_L of a transmission line are connected together by the relation :

(A)
$$k_r = \frac{Z_L + Z_0}{Z_0 - Z_L}$$

(B) $k_r = \frac{Z_L Z_0}{Z_0 - Z_L}$
(C) $k_r = \frac{Z_L - Z_0}{Z_0 + Z_L}$
(D) $k_r = \frac{Z_L - Z_0}{Z_0 Z_L}$

- 31. Using Biot-Savart law, the magnetic induction at a distance d, from an infinitely long straight wire in which current I is flowing along the z-direction, is :
 - (A) $(M_0 / 4\pi)\hat{k}$
 - (B) (M₀ / 4 π)(2I / d) \hat{k}
 - (C) $(M_0 / 4\pi)(I / d)\hat{k}$
 - (D) $(M_0 I / 4\pi)\hat{k}$
- 32. Magnitude of electric field at large distance r, from an ideal electric dipole is proportional to :
 - (A) r^2 (B) r^{-2} (C) r^{-3} (D) r^{-4}
- 33. At the uncharged interface between two linear dielectrics with permitivities \in_1 and \in_2 , electric fields $\overline{E_1}$ and $\overline{E_2}$ make angles θ_1 and θ_2 with the normal. The ratio \in_1 / \in_2 is equal to :
 - (A) $tan\theta_1/tan\theta_2$
 - (B) $\sin\theta_1/\sin\theta_2$
 - (C) $\cos\theta_1/\cos\theta_2$
 - $(D) \ cot\theta_1/cot\theta_2$

- 34. Charge Q is divided into two parts which are then kept at distance d apart. The force between them will be maximum if the charges on two parts are :
 - (A) Q/4 and 3Q/4
 - (B) Q/3 and 2Q/3 $\,$
 - (C) Q/2 and Q/2
 - (D) any q_1 and q_2 such that $q_1 + q_2 = Q; q_1 > 0, q_2 > 0$
- 35. For uniformly charged solid sphere of radius R, which of the following statements is correct about the magnitude of electric field at a distance r from the center of the sphere ?

(A) $\mathbf{E} = \mathbf{0}$ for $r < \mathbf{R}$

- (B) E = non-zero constant for r < R
- (C) E proportional to r, for r < R
- (D) E proportional to 1/r, for r < R

- 36. A particle of mass *m* is confined in a three-dimensional cubical box of size L. The number of eigenstates of the Hamiltonian with energy $\frac{19\hbar^2\pi^2}{mL^2}$ is : (A) 10 (B) 4 (C) 3 (D) 9
- 37. Consider an anisotropic twodimensional oscillator given by the Hamiltonian

$$H = -\frac{\hbar^2}{2m} \left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right) + \frac{1}{2} m \omega^2 x^2 + 2m \omega^2 y^2$$

The eigen energy of the oscillator is given by :

- (A) $E_n = (n + 3 / 2)\hbar\omega$ (B) $E_n = (n + 1)\hbar\omega$
- (C) $\mathbf{E}_n = (2n+1)\hbar\omega$
- (D) $E_n = (n + 2 / 3)\hbar\omega$

38. For a one-dimensional harmonic oscillator, a⁺ and a are raising and lowering operators and |n > is the nth energy eigenstate. Then a⁺ a |n + 1> is equal to :

(A)
$$(n+1) \mid n >$$

- (B) n | n + 1 >
- (C) $\sqrt{n(n+1)} | n+1 >$

(D)
$$(n + 1) | n + 1 >$$

39. If \overline{A} and \overline{B} are quantum mechanical operators, then $\left[\left[\overline{A},\overline{B}\right],\left[\overline{B},\overline{A}\right]\right]$ is equal to : (A) $\overline{A} \overline{B} \overline{B} \overline{A} - \overline{B} \overline{A} \overline{A} \overline{B}$ (B) 0 (C) $\overline{A} \overline{A} \overline{B} - \overline{B} \overline{B} \overline{A}$ (D) $[A, B]^2$

40. Sixteen non-interacting electrons are confined in an infinite box of side *a*. The energies of the least energetic and the most energetic electrons in the ground state of the system are :

(A)
$$\frac{\hbar^2 \pi^2}{2ma^2}, \frac{32\hbar^2 \pi^2}{ma^2}$$

(B) 0, $\frac{32\hbar^2 \pi^2}{ma^2}$
(C) $\frac{\hbar^2 \pi^2}{2ma^2}, \frac{\hbar^2 \pi^2}{2ma^2}$

(D)
$$\frac{n^{-}\pi^{-}}{2ma^{2}}, \frac{128n^{-}\pi^{-}}{ma^{2}}$$

41. Using the triangular trial wave function :

 $\psi(x) = \begin{cases} Ax & \text{for } 0 \le x \le a / 2 \\ A(a-x) & \text{for } \frac{a}{2} \le x \le a \\ 0 & \text{otherwise} \end{cases}$

an upper bound on the ground state energy of the one-dimensional infinite square well is :

(A)
$$\frac{8\hbar^2}{ma^2}$$
 (B) $\frac{7\hbar^2}{ma^2}$
(C) $\frac{6\hbar^2}{ma^2}$ (D) $\frac{5\hbar^2}{ma^2}$

- 42. A hydrogen atom is perturbed by a potential $H_1 = bx^2$. The first order correction to ground state energy is $(a_0 \text{ is the Bohr radius})$:
 - (A) ba_0^2 (B) $2ba_0^2$ (C) $ba_0^2/2$ (D) $ba_0^2/4$
- 43. Consider a particle of mass m in a one-dimensional box with walls at x = 0 and x = L with ground state energy E_1 . If the separation between the walls is adiabatically (slowly) increased to 2L, the change in the ground state energy is given by :

(A) 0 (B)
$$\frac{2}{3}E_1$$

(C)
$$\frac{3}{8} E_1$$
 (D) $\frac{3}{2} E_1$

44. In scattering theory of spherically symmetric potential, the incident particles on z-axis are represented by :

(A) A exp (*ikz*)
(B) A
$$\frac{\exp(ikz)}{r}$$

(C) A $r \exp(ikz)$
(D) A $\frac{\exp(ikz)}{r^2}$

45. Using WKB approximation, the allowed energies E_n , (n = 1, 2, 3...) for a one-dimensional harmonic oscillator are :

(A)
$$\left(n - \frac{1}{2}\right)\hbar\omega$$

(B) $\left(n + \frac{1}{2}\right)\hbar\omega$
(C) $(2n - 1) \hbar\omega$
(D) $(2n + 1) \hbar\omega$

- 46. Two Stern-Gerlac apparatus S_1 and S_2 are kept along the *z*-axis with the directions of their magnetic fields along the positive *x* and *y* directions respectively. Each apparatus allows only those particles to pass which have their spins aligned in the direction of its magnetic field. If an unpolarised beam of spin $\frac{1}{2}$ particles is made incident on S_1 , the ratio of the intensities $I_i : I_f$ of the initial and final beams is :
 - $(A) \ 8 : 1 \qquad (B) \ 4 : 1$
 - $(C) \ 1 \, : \, 0 \qquad \qquad (D) \ 2 \, : \, 1$

47. For Klein-Gordon equation, the probability current density is given by :

(A)
$$\frac{i\hbar c}{2m} (\psi \nabla \psi^* - \psi^* \nabla \psi)$$

(B)
$$\frac{i\hbar}{2m} (\psi \nabla \psi^* - \psi^* \nabla \psi)$$

(C)
$$\frac{i\hbar}{2m} (\psi \nabla \psi^* + \psi^* \nabla \psi)$$

(D)
$$\frac{i\hbar}{2mc} \left(\psi \nabla \psi^* - \psi^* \nabla \psi \right)$$

48. A particle of mass m is confined in an infinite square well with a shelf of height V_0 extending half way across so that :

$$\mathbf{V}(x) = \begin{cases} V_0 & \text{ for } 0 < x < a \ / \ 2 \\ 0 & \text{ for } \frac{a}{2} < x < a \\ \infty & \text{ otherwise} \end{cases}$$

Using WKB approximation, the allowed energies $E_n (n = 1, 2, 3,...)$ for this particle are, (given $E_n^0 = n^2 \pi^2 \hbar^2 / 2ma^2$ are the energies of particle in an infinite well with no shelf) :

(A)
$$E_n^0 + V_0$$

(B) $E_n^0 + V_0 / 2$
(C) $E_n^0 + \frac{V_0}{2} \left(1 + \frac{V_0}{4E_n^0} \right)$
(D) $E_n^0 + \frac{V_0}{2} \left(1 + \frac{V_0}{8E_n^0} \right)$

- 49. In a one-dimensional random walk, the probability of step of unit length in positive direction is 2/3 and in negative direction is 1/3. The mean displacement of the walker after nsteps is :
 - (A) *n*/8 (B) 2*n*/3
 - (C) *n*/3 (D) 0
- 50. In a two-state system, one with energy 0 and other with energy $\varepsilon > 0$. The system will have both the levels equally occupied when :
 - (A) T = 0
 - (B) T is infinite
 - (C) T is very low
 - (D) T is very high
- 51. A system of three indistinguishable particles has a total energy of 4ε . There are four single particle energy states with energies 0, ε , 2ε and 3ε . The number of microstates accessible to the system will be :
 - (A) 4 (B) 1
 - (C) 2 (D) 3

- 52. The temperature T of a blackbody enclosure is doubled, then the total number of photons inside the enclosure increases by a factor of :
 - (A) 2
 (B) 4

 (C) 8
 (D) 16
- 53. For an adiabatic process involving having volume gas V and temperature T, which of the following is constant (here $\gamma = C_p/C_v$) : TV^{γ} (A) TV (**B**) (C) $TV^{\gamma-1}$ Τγν (D)
- 54. Helmholtz free energy function is defined by :

 (A) F = U + TS
 (B) F = U + TS
 (B) F = U TS
 (C) F = U + PV
 (D) F = U + PV TS

 55. The Maxwell-Boltzmann distribution holds for :

 (A) distinguishable particles
 (B) all indistinguishable particles
 (C) nerticles with helf interval axis
 - (C) particles with half integral spin
 - (D) particles with integral spin For all the quantum states with

(D)

100 K

- 56. For all the quantum states with energy greater than Fermi energy to be empty in a Fermi-Dirac system, the temperature should be :
 (A) 273 K (B) 373 K
 - (C) 0 K

57. Fluctuation of magnetization M, given as $\Delta M = \frac{\sqrt{\langle M^2 \rangle - \langle M \rangle 2}}{\langle M \rangle}$ for N magnetic moments μ with two allowed orientation $\pm M$ in an external field H at temperature T is :

(A)
$$\Delta M = \frac{1}{\sqrt{N} \cosh\left(\frac{\mu H}{KT}\right)}$$

(B)
$$\Delta M = \frac{1}{\sqrt{N} \tanh\left(\frac{\mu H}{KT}\right)}$$

(C)
$$\Delta M = 1 / \sqrt{N}$$

(D)
$$\Delta M = \frac{1}{\sqrt{N} \sinh\left(\frac{\mu H}{KT}\right)}$$

- 58. Consider ideal Fermi gas in three dimensions. The density of energy states ε is proportional to :
 - $\begin{array}{cccc} (A) & \epsilon^{1/2} & (B) & \epsilon^{-1/2} \\ (C) & \epsilon^{0} & (D) & \epsilon^{2} \end{array}$

59. Consider a system of two Ising spins

 S_1 and S_2 taking values ± 1 with interaction energy E = $-JS_1S_2.$ For large temperature T, the average energy of the system varies as $C/(k_BT)$ with C given by :

- (A) $-J^2$ (B) $-2J^2$
- (C) J^2 (D) $4J^2$

60. For the following transistor circuit assume $V_{BE} = 0.7V$, $\beta_{dc} = 100$; then the current flowing through R_E is :

$$R_{\rm B} = 1.0 \text{ k}\Omega$$

 $R_{\rm E} = 1.0 \text{ k}\Omega$
 $R_{\rm E} = 1.0 \text{ k}\Omega$
 $R_{\rm E} = 1.0 \text{ k}\Omega$
 $-V_{\rm EE} = 5.0 \text{ V}$

- (A) 4.0 mA
 (B) 8.0 mA
 (C) 4.3 mA
 (D) 3.6 mA
- 61. For the following differential amplifier circuit, the output voltage V_{out} is :



(A)
$$+10.0$$
 V
(B) -10.0 V
(C) -1.0 V

62. In the following circuit, the transistor functions as :



- (A) OR gate (B) AND gate
- (C) NOR gate (D) NAND gate
- 63. Identify the function 'F' generatedby the logic network shownbelow :



- (A) $\mathbf{F} = (\mathbf{A} + \mathbf{B}) \mathbf{C}$
- $(B) \quad F = C + B + \overline{B}A$
- (C) F = BC (B + A)
- (D) F = ABC

64. The following digital circuit acts as a :



- (A) Half-Subtractor
- (B) Half-Adder
- (C) Half-Adder/Subtractor
- (D) 2's complement Adder/ Subtractor
- 65. For the following diode circuit, the voltage drop across each diode is0.7 V. The current flowing through the resistor R is

- 66. When the modulating signal controls the amplitude of a carrier wave, it is known as :
 - (A) frequency modulation
 - (B) amplitude modulation
 - (C) phase modulation
 - (D) pulse amplitude modulation
- 67. A digital multimeter normally uses :
 - (A) Flash ADC
 - (B) counter ADC
 - (C) Successive approximation ADC
 - (D) Duel slope ADC
- 68. Which of the following gauge is used to calibrate gauges employed to measure low pressure of the order of 1.0×10^{-6} torr ?
 - (A) Pirani gauge
 - (B) Penning gauge
 - (C) Thermocouple gauge
 - (D) McLeod gauge

- 69. The difference between the indicated value and true value of a quantity is known as :
 - (A) Gross error
 - (B) Absolute error
 - (C) Dynamic error
 - (D) Relative error
- 70. The ratio of frequencies of the first line of the Lyman series and the first line of the Balmer series is :
 (A) 4/27 (B) 8/27
 (C) 27/5 (D) 27/8
- 71. The number of fundamental vibrational modes of CO_2 molecule is :
 - (A) Four : 2 are Raman active and2 are infrared active
 - (B) Four : 1 is Raman active and3 are infrared active
 - (C) Three : 1 is Raman active and2 are infrared active
 - (D) Three : 2 are Raman active and1 is infrared active

- 72. A Co^{2+} ion has the spectroscopic term factor :
 - (A) ${}^{6}S_{5/2}$ (B) ${}^{4}F_{3/2}$ (C) ${}^{5}D_{0}$ (D) ${}^{4}F_{5/2}$
- 73. The coherence length of laser light is :
 - (A) directly proportional to the length of the active lasing medium
 - (B) inversely proportional to the width of the spectral line
 - (C) directly proportional to the width of the spectral line
 - (D) inversely proportional to the length of the active lasing medium
- 74. The g_N value for F¹⁹ nucleus is
 5.256. If it is placed in a magnetic field of strength 1.0 T, the relative population in two spin states at 300 K will be,

(Given $\mu_N = 5.05 \times 10^{-27} \text{ JT}^{-1}$ and $k = 1.38 \times 10^{-23} \text{ JK}^{-1}$) : (A) 1.0 (B) 2.0

(C) 0.5 (D) 2.5

- 75. Frank-Condon principle predicts large intensity spectral line for electronic transitions :
 - (A) in monoatomic gases
 - (B) between the vibrational energy levels of any electronic state
 - (C) between the vibrational energy levels of two electronic states of a constant internuclear separation
 - (D) between the v = 0 vibrational levels of the two electronic states
- 76. If the average separation between the adjacent lines in the rotational IR spectrum of CO molecule is 3.844 cm⁻¹, then the value of rotational constant is :
 - (A) 7.688 cm⁻¹ (B) 1.922 cm⁻¹ (C) 3.844 cm⁻¹
 - (D) 5.766 cm^{-1}

79. The D_1 and D_2 lines of sodium 77. An electron in atomic hydrogen has $(^2P_{1/2} \rightarrow \ ^2S_{1/2} \mbox{ and } \ ^2P_{3/2} \rightarrow \ ^2S_{1/2})$ g = 2.0032. In an ESR spectrometer will split on application of a weak magnetic field into : at 9.250 GHz, two lines from the H (A) 3 lines each atom appeared at 353.3 mT and (B) 6 lines each 306.6 mT. The hyperfine coupling (C) 4 lines each (D) 4 and 6 lines, respectively constant will be : 80. The first reflection from FCC crystal (A) $1.6 \times 10^9 \text{ Hz}$ is observed at Bragg angle $\theta = 21.5^{\circ}$, the θ corresponding to the second (B) $1.6 \times 10^{10} \text{ Hz}$ reflection is : (C) 3.2×10^9 Hz (A) 13.5° (**B**) 18.5° (C) 25.0° (D) 36.8° (D) $3.2 \times 10^{10} \text{ Hz}$ 81. A pair of Li^+ and Cl^- ions, with their 78. Relative intensities of successive radii 0.60 Å and 1.81 Å respectively, touch each other. The attractive lines in the observed Raman spectra force between them is : of nitrogen molecule is : (A) 1.96×10^{-9} N (B) 2.96×10^{-9} N (A) 3 : 4(**B**) 1:2(C) 3.96×10^{-9} N (C) 2:3(D) 1:3(D) 4.96×10^{-9} N

- 82. Heat capacity C_v of a metal is measured as a function of temperature T in the low temperature region. Assume that the measured C_v is due to both electronic and lattice contributions, then the plot of (C_v/T) versus T is :
 - (A) linear in T
 - (B) quadratic in T
 - (C) cubic in T
 - (D) inversely proportional to T
- 83. The number of independent elastic constants in an isotropic cubic solid is :
 - (A) 1 (B) 2
 - (C) 3 (D) 4
- 84. For an intrinsic semiconductor, m_e^* and m_h^* are respectively the effective masses of electrons and holes near the corresponding band edges. At a finite temperature, the position of the Fermi level :

(A) depends on m_e^* but not on m_h^*

- (B) depends on m_h^* but not on m_e^*
- (C) depends on both m_e^* and m_h^*
- (D) depends neither on m_e^* nor on m_h^*

- 85. A solid superconductor of type I is placed in an external magnetic field and is then cooled below its critical temperature. The superconductor :
 - (A) retains its magnetic flux because the surface current supports it
 - (B) expels out its magnetic flux because it behaves like a paramagnetic material
 - (C) expels out its magnetic flux because it behaves like an antiferromagnetic material
 - (D) expels out its magnetic flux because the surface current induces a field in the direction opposite to the applied field
- 86. The dispersion relation for a simple cubic crystal is given by :

$$\mathbf{E}(\vec{k}) = \mathbf{E}_0 - 2\beta$$
$$(\cos k_x a + \cos k_y a + \cos k_z a),$$

where β is constant having dimension of energy and α is lattice constant. The width of the energy band is :

(A) 2β	(B)	4β
(C) 8β	(D)	12β

- 87. Consider the energy E in the Brillouin zone as a function of the magnitude of the wave vector \vec{k} for a crystal of lattice constant 'a'. Then:
 - (A) the slope of E versus k is proportional to the group velocity
 - (B) the slope of E versus k has its maximum value at $|\vec{k}| = \pi / a$
 - (C) the plot of E versus k will be parabolic in the interval $-\pi / a < k < \pi / a$
 - (D) the slope of E versus k is nonzero for all k in the interval $-\pi / a < k < \pi / a$
- 88. Eu^{3+} ion has outer electronic configuration $4f^{6}5s^{2}5p^{6}$. Its ground state is characterized by one of the following spectroscopic terms :
 - (A) ${}^{7}F_{0}$ (B) ${}^{8}S_{7/2}$
 - (C) ${}^{7}F_{6}$ (D) ${}^{6}H_{15/2}$

- 89. If the static dielectric constant of NaCl crystal is 5.6 and its optical refractive index is 1.5, the ratio of its ionic polarizability to its total polarizability is :
 - (A) 0.5
 (B) 0.7
 (C) 0.8
 (D) 0.9
- 90. A lattice is characterized by the following primitive vectors $\vec{a} = 2(\hat{i} + \hat{j}), \qquad \vec{b} = 2(\hat{j} + \hat{k}),$ $\vec{c} = 2(\hat{k} + \hat{i}).$

The reciprocal lattice corresponding to the above is :

- (A) fcc with cube edge 2π
- (B) bcc with cube edge π
- (C) bcc with cube edge 2π
- (D) fcc with cube edge π
- What is the binding energy per 91. nucleon for isotope $\frac{55}{25}$ Mn ? (Given : M_N = 1.008665 amu, 551.007825 $M_p =$ amu, 25 Mn = 54.938050 amu(A) 8.7 MeV (B) 9.2 MeV (C) 9.5 MeV (D) 9.9 MeV

- 92. What should be the energy required, if an electron is used as a probe for studying the nuclear structure, shape and distribution. (Consider nuclear radius is 10^{-13} cm) :
 - (A) 0.1 GeV (B) 0.2 GeV
 - (C) 0.3 GeV (D) 0.4 GeV
- 93. To penetrate the Coulomb barrier of a light nucleus (¹₁H), a proton must have a minumum energy of the order of (Consider radius of nucleus ~ 1Fm) :

(A) 1.44 TeV (B) 1.44 GeV

(C) 1.44 MeV (D) 1.44 KeV

94. What is the energy released in the following nuclear reaction :

$${}_{3}^{6}\text{Li} + {}_{1}^{2}\text{H} \rightarrow 2 \; {}_{2}^{4}\text{He} + \text{Q}$$
(Given : ${}_{3}^{6}\text{Li} = 6.01693 \text{ amu}$
 ${}_{1}^{2}\text{H} = 2.01471 \text{ amu},$
 ${}_{2}^{4}\text{He} = 4.00388 \text{ amu}$)
(A) 11.4 MeV (B) 22.4 MeV
(C) 33.4 MeV (D) 44.4 MeV

95. The quark content of baryon Ξ^0 with strangeness S = -2 is given by :

(A)	$u \overline{s} \overline{s}$	(B)	$d \ s \ s$
(C)	$d \overline{s} \overline{s}$	(D)	uss

- 96. Experimentally it is observed that neutron (n)-proton(p) system (deuteron) is bound, but the protonproton and neutron-neutron systems are not bound. This is due to :
 - (A) unequal nuclear force between *n-p*, *n-n* and *p-p* systems
 - (B) unequal total charges of *n-p*, *n-n* and *p-p* systems
 - (C) Pauli's principle
 - (D) non-conservation of angular momentum
- 97. In the nuclear shell model, orbitals are filled in the following order ${}^{1}s_{1/2}$, ${}^{1}p_{3/2}$, ${}^{1}p_{1/2}$, ${}^{1}d_{5/2}$, ${}^{2}s_{1/2}$, ${}^{1}d_{3/2}$, etc. The splitting between the $p_{3/2}$ and $p_{1/2}$ orbitals is caused by:
 - (A) angular momentum of the nucleus
 - (B) only the spins of the nucleus
 - (C) spin-orbit coupling of the nucleus
 - (D) angular momentum and spin of the nucleus

98. Based on the additive quantum numbers such as strangeness (S), baryon number (B), charge (Q), and isospin (I), indicate for which among the four options given below, the following nuclear reaction cannot be induced

 $\Pi^+ + n \rightarrow \Pi^{o} + \mathbf{K}^+$

- (A) Q, B, S are conserved, but I_3 is not conserved
- (B) Q and B are conserved, but S and ${\rm I}_3$ are not conserved
- (C) Q and I_3 are conserved, but B and S are not conserved
- (D) B, S and I_3 are conserved, but Q is not conserved
- 99. Parity is not conserved in :
 - (A) strong nuclear interactions
 - (B) gravitational interactions
 - (C) weak interactions
 - (D) electromagnetic interactions

- 100. Parity non-conservation was established in β -decay when it was observed that from polarised Co⁶⁶ nuclei :
 - (A) electrons were emitted equally

in all directions

(B) more electrons were emitted in

direction opposite to that of

magnetic field

(C) electrons were not emitted in

any direction

(D) more electrons were emitted

perpendicular to the direction of

magnetic field

ROUGH WORK