Test Booklet Code & Serial No. प्रश्नपत्रिका कोड व क्रमांक

В

Paper-II PHYSICAL SCIENCE

Sign	nature and Name of Invigilator	Seat No.
1. (Signature)		(In figures as in Admit Card)
(N	Vame)	Seat No.
2. (Signature)		(In words)
(N	Jame)	OMR Sheet No.
JUN - 32219		(To be filled by the Candidate)
		•
Time Allowed : 2 Hours]		[Maximum Marks : 200
Number of Pages in this Booklet: 32		Number of Questions in this Booklet : 100
1. 2. 3.	Instructions for the Candidates Write your Seat No. and OMR Sheet No. in the space provided on the top of this page. This paper consists of 100 objective type questions. Each question will carry two marks. All questions of Paper II will be compulsory. At the commencement of examination, the question booklet will be given to the student. In the first 5 minutes, you are requested to open the booklet and compulsorily examine it as follows: (i) To have access to the Question Booklet, tear off the paper seal on the edge of this cover page. Do not accept a booklet without sticker-seal or open booklet. (ii) Tally the number of pages and number of questions in the booklet with the information printed on the cover page. Faulty booklets due to missing pages/questions or questions repeated or not in serial order or any other discrepancy should not be accepted and correct booklet should be obtained from the invigilator within the period of 5 minutes. Afterwards, neither the Question Booklet will be replaced nor any extra time will be given. The same may please be noted. (iii) After this verification is over, the OMR Sheet Number should be entered on this Test Booklet. Each question has four alternative responses marked (A), (B), (C) and (D). You have to darken the circle as indicated below on the correct response against each item. Example: where (C) is the correct response.	विद्यार्थ्यांसाठी महत्त्वाच्या सूचना 1. परिक्षार्थींनी आपला आसन क्रमांक या पृष्ठावरील वरच्या कोप-यात लिहावा. तसेच आपणांस दिलेल्या उत्तरपत्रिकेचा क्रमांक त्याखाली लिहावा. 2. सदर प्रश्नपत्रिकेत 100 बहुपर्यायी प्रश्न आहेत. प्रत्येक प्रश्नास दोन गुण आहेत. या प्रश्नपत्रिकेतील सर्व प्रश्न सोडविणे अनिवार्य आहे. 3. परीक्षा सुरू झाल्यावर विद्यार्थ्याला प्रश्नपत्रिका दिली जाईल. सुरुवातीच्या 5 मिनीटांमध्ये आपण सदर प्रश्नपत्रिका उघडून खालील बाबी अवश्य तपासून पहाव्यात. (i) प्रश्नपत्रिका उघडण्यासाठी प्रश्नपत्रिकेवर लावलेले सील उघडावे. सील नसलेली किंवा सील उघडावेली प्रश्नपत्रिकेची एकूण पृष्ठे तसेच प्रश्नपत्रिकेतील एकूण प्रश्नांची संख्या पडताळून पहावी. पृष्ठे कमी असलेली/कमी प्रश्न असलेली/प्रश्नांचा चुकीचा क्रम असलेली किंवा इतर त्रुटी असलेली सदोष प्रश्नपत्रिका सुरुवातीच्या 5 मिनिटातच पर्यवेक्षकाला परत देऊन दुसरी प्रश्नपत्रिका मागवून घ्यावी. त्यानंतर प्रश्नपत्रिको बदलून मिळणार नाही तसेच वेळही वाढवून मिळणार नाही तसेच वेळही वाढवून मिळणार नाही राची कृपया विद्यार्थानी नोंद घ्यावी. (iii) वरीलप्रमाणे सर्व पडताळून पाहिल्यानंतरच प्रश्नपत्रिकेचर ओ.एम.आर. उत्तरपत्रिकेचा नंबर लिहावा. 4. प्रत्येक प्रश्नासाठी (A), (B), (C) आणि (D) अशी चार विकल्प उत्तरे दिली आहेत. त्यातील योग्य उत्तराचा रकाना खाली दर्शविल्याप्रमाणे ठळकपणे काळा/निळा करावा.
	A B D	उदा. : जर (C) हे योग्य उत्तर असेल तर.
5.	Your responses to the items are to be indicated in the OMR Sheet given inside the Booklet only. If you mark at any place other than in the circle in the OMR Sheet, it will not be evaluated.	A B D 5. या प्रश्नपत्रिकेतील प्रश्नांची उत्तरे ओ.एम.आर. उत्तरपत्रिकेतच दर्शवावीत.
6.	Read instructions given inside carefully. Rough Work is to be done at the end of this booklet.	इतर ठिकाणी लिहिलेली उत्तरे तपासली जाणार नाहीत.
7. 8.	If you write your Name, Seat Number, Phone Number or put	 आत दिलेल्या सूचना काळजीपूर्वक वाचाव्यात. प्रश्नपत्रिकेच्या शेवटी जोडलेल्या कोऱ्या पानावरच कच्चे काम करावे.
9.	any mark on any part of the OMR Sheet, except for the space allotted for the relevant entries, which may disclose your identity, or use abusive language or employ any other unfair means, you will render yourself liable to disqualification. You have to return original OMR Sheet to the invigilator at the	 प्रश्नपात्रकच्या शवटा जाडलल्या काऱ्या पानावरच कच्च काम कराव. जर आपण ओ.एम.आर. वर नमूद केलेल्या ठिकाणा व्यतिरीक्त इतर कोठेही नाव, आसन क्रमांक, फोन नंबर किंवा ओळख पटेल अशी कोणतीही खूण केलेली आढळून आल्यास अथवा असभ्य भाषेचा वापर किंवा इतर गैरमार्गांचा अवलंब केल्यास विद्यार्थ्याला परीक्षेस अपात्र ठरविण्यात येईल.
10.	end of the examination compulsorily and must not carry it with you outside the Examination Hall. You are, however, allowed to carry the Test Booklet and duplicate copy of OMR Sheet on conclusion of examination. Use only Blue/Black Ball point pen.	 परीक्षा संपल्यानंतर विद्यार्थ्याने मूळ ओ.एम.आर. उत्तरपत्रिका पर्यवेक्षकांकडे परत करणे आवश्यक आहे. तथापि, प्रश्नपत्रिका व ओ.एम.आर. उत्तरपत्रिकेची द्वितीय प्रत आपल्याबरोबर नेण्यास विद्यार्थ्यांना परवानगी आहे. फक्त निळ्या किंवा काळ्या बॉल पेनचाच वापर करावा.
11.	Use of any calculator or log table, etc., is prohibited.	 कलक्युलटर किवा लाग टबल वापरण्यास परवानगा नाहा. चुकीच्या उत्तरासाठी गुण कपात केली जाणार नाही.
12.	There is no negative marking for incorrect answers.	3 3

12.

There is no negative marking for incorrect answers.

Physical Science Paper II

Time Allowed: 120 Minutes] [Maximum Marks: 200 Note: This Paper contains Hundred (100) multiple choice questions. Each question carrying Two (2) marks. Attempt All questions.

- 1. Current I is flowing through an infinitely long wire placed along the x-axis. The Cartesian coordinates of the points A and B are A(2, 3, -4) and B = (-8, 4, -3). The ratio of magnitudes of \overline{B} at point A to that at point B is :
 - (A) $\mu_0 I$
 - (B) $\frac{1}{4}$
 - (C) $\frac{4}{1}$
 - (D) 1
- 2. There is a space region where $\overline{E} = E_0 \hat{z} \quad \text{and} \quad \overline{B} = B_0 \hat{x} \quad \text{are both}$ present. A charged particle with velocity $\left(\frac{E_0}{B_0}\right) \hat{y}$ enters this region.

The trajectory of the particle in this region is a :

- (A) Straight line
- (B) Circle
- (C) Cycloid
- (D) Circular helix

- 3. The magnetic dipole moment of a circular loop of radius R, carrying current I, is \overline{m} . If radius is doubled and current is halved, then the magnetic dipole moment becomes :
 - (A) 4m
 - (B) $\frac{m}{4}$
 - (C) $\frac{m}{2}$
 - (D) 2m
- 4. A rectangle of cross-sectional area 'A' is placed in a uniform constant electric field \overline{E} . The plane of the rectangle makes an angle of 30° with the direction of the electric field. The electric flux through the rectangle is:
 - (A) AE
 - (B) $\frac{AE}{2}$
 - (C) $AE\frac{\sqrt{3}}{2}$
 - (D) Zero

- 5. The magnitude of magnetic vector potential at a distance r from an ideal magnetic quadrupole is proportional to:
 - (A) r^{-1}
 - (B) r^{-2}
 - (C) r^{-3}
 - (D) r^{-4}
- 6. ABCD is a square and 'O' is the point of intersection of the diagonals.
 Charge Q is placed at corner A and charge Q is placed at corner C. If electric potential at corner D is 1 V, then the electric potential at point 'θ' is:
 - (A) Zero V
 - (B) 1 V
 - (C) $\frac{1}{\sqrt{2}}$ V
 - (D) $\left(1+\frac{1}{\sqrt{2}}\right)V$

- 7. A constant current I is flowing through a cylindrical conductor. The direction of Poynting vector on the curved surface is:
 - (A) \hat{z}
 - (B) **ô**
 - (C) \hat{r}
 - (D) $-\hat{r}$
- 8. Vector potential $\overline{A}(\overline{r}, t)$ is such that $\overline{r}.\overline{A} = \frac{-\mu_0}{4\pi} \frac{Q}{r^2}.$ The corresponding electric potential $V(\overline{r}, t)$, under Lorentz gauge condition is :
 - (A) $\frac{Q}{4\pi\epsilon_0 r}$
 - (B) $\frac{\mathbf{Q}}{4\pi\varepsilon_0 r^2}$
 - (C) $\frac{Qt}{4\pi\epsilon_0 r}$
 - (D) $\frac{\mathbf{Q}t}{4\pi\varepsilon_0 r^2}$

- 9. If an electromagnetic wave is propagating in a medium with permittivity ϵ and permeability μ , then $\sqrt{\frac{\mu}{\epsilon}}$ is:
 - (A) The refractive index of the medium.
 - (B) The square root of the refractive index of the medium.
 - (C) The intrinsic impedance of the medium.
 - (D) The energy density of the wave in the medium.
- 10. A plane electromagnetic wave is propagating through a perfect dielectric medium with dielectric constant equal to π . The phase difference between \overline{E} and \overline{B} associated with the wave is :
 - (A) Zero
 - (B) $\frac{\pi}{4}$
 - (C) $\frac{\pi}{2}$
 - (D) π

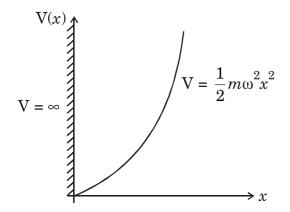
- 11. A boy of mass 60 kg is running with a velocity 12 km/hr. The de Broglie wavelength associated with him is approximately ($h = 6.626 \times 10^{-34} \text{ Js}$):
 - (A) $3 \times 10^{-32} \text{ m}$
 - (B) $3 \times 10^{-34} \text{ m}$
 - (C) 3×10^{-30} m
 - (D) $3 \times 10^{-31} \text{ m}$
- 12. Which of the following functions can be an acceptable solution for Schrödinger equation for all values of x?
 - (A) $\psi(x) = Ae^{-\alpha x^2}$
 - (B) $\psi(x) = Ae^{\alpha x^2}$
 - (C) $\psi(x) = A \tan x$
 - (D) $\psi(x) = A \sec x$

- 13. The Hamiltonian $H = \frac{-\hbar^2}{2m} \frac{d^2}{dx^2} \alpha \delta(x)$ is given for a particle. Using the trial wave function $\psi_{\text{trial}}(x) = Ae^{-bx^2}$ (with b as the variational parameter), the bound on the ground state energy is :
 - (Given: $\int_{-\infty}^{\infty} x^{2n} e^{-\alpha x^2} dx$
 - (A) $-m\alpha^2/2\hbar^2$
 - (B) $-2m\alpha^2/\pi\hbar^2$
 - (C) $-m\alpha^2/\pi\hbar^2$
 - (D) $m\alpha^2/\pi\hbar^2$

- 14. A particle is moving in a one-dimensional infinite potential well of width a. Using a normalized trial wave function $\psi(x) = \frac{\sqrt{15}}{4a^{5/2}}(a^2-x^2)$, variational calculation estimate for $4a^{5/2}$ the ground state energy is :
 - (A) $\frac{5\hbar^2}{4ma^2}$
 - (B) $\frac{3\hbar^2}{2ma^2}$
 - (C) $\frac{3\hbar^2}{5ma^2}$
 - (D) $\frac{5\hbar^2}{2ma^2}$

 $+\sqrt{2}\psi_{21-1}$

15. A particle is constrained to move in a truncated harmonic potential well (as shown below). Which one of the following statements is *correct*?



- (A) The parity of the first excited state is even.
- (B) The parity of the ground state is even.
- (C) The ground state energy is $\frac{1}{2}\hbar\omega$
- (D) The energy of the first excited state is $\frac{7}{2}\hbar\omega$

16. The wave function for an electron in a hydrogen atom is given by $\psi(r) = \psi_{200}(r) + 2\psi_{211} + 3\psi_{210}$

where $\psi_{n_{l}m_{l}}(\vec{r})$ is the wave function for an electron in the eigenstate $(n_{l}m_{l})$. The expectation value of z-component of angular momentum, <L $_{z}>$ in the state $\overset{\rightarrow}{\psi(r)}$ is :

- (A) $3\hbar/8$
- (B) $\hbar/8$
- (C) 11ħ/16
- (D) $15\hbar/16$

7

17. A system described by the Hamil-

tonian H =
$$\begin{pmatrix} 5 & 2 & 0 \\ 2 & 5 & 0 \\ 0 & 0 & 2 \end{pmatrix}$$
 is perturbed

by
$$H' = \epsilon \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & -1 \\ 1 & -1 & 1 \end{pmatrix}$$
 where

 $(\epsilon << 1)$. A pair of eigenvalues of the perturbed system is :

- (A) $3 + 2\varepsilon$, $2 + \varepsilon$
- (B) $3, 2 + 2\varepsilon$
- (C) 3, $7 + 2\varepsilon$
- (D) $3 + 2\epsilon, 7 + 2\epsilon$
- 18. An electron is in a state $\chi = \begin{pmatrix} \frac{1+i}{\sqrt{6}} \\ \sqrt{2} / \sqrt{3} \end{pmatrix}$

where the basis functions are $\begin{pmatrix} 1 \\ 0 \end{pmatrix}$

and $\begin{pmatrix} 0 \\ 1 \end{pmatrix}$. The respective probabilities that a measurement of S_z yields values $+\hbar/2$ and $-\hbar/2$ are :

- (A) $\frac{1}{2}$ and $\frac{1}{2}$
- (B) $\frac{2}{3}$ and $\frac{1}{3}$
- (C) $\frac{1}{4}$ and $\frac{3}{4}$
- (D) $\frac{1}{3}$ and $\frac{2}{3}$

19. The differential scattering crosssection for a Gaussian potential $V(r) = V_0 e^{-r^2/a^2}$, using Born approximation is given by

$$\sigma(\theta) = Ce^{D\sin^2(\theta/2)}$$

where C and D are constants and (C and D > 0) $\sigma(\theta)$ is maximum for θ =

- (A) π
- (B) 2π
- (C) 3π
- (D) $2n\pi$, where n = 0, 1, 2, ...
- 20. A particle is in the normalized state $|\psi\rangle$. $|\psi\rangle$ is a superposition of energy eigen states $|E_0| = 10 \text{ eV}\rangle$ and $|E_1| = 30 \text{ eV}\rangle$. The average value of energy of the particle in the state $|\psi\rangle$ is 20 eV. The state $|\psi\rangle$ is:

(A)
$$\frac{1}{2} | E_0 = 10 \text{ eV} > + \frac{\sqrt{3}}{4} | E_1 = 30 \text{ eV} >$$

(B)
$$\frac{1}{\sqrt{3}} | E_0 = 10 \text{ eV} > + \sqrt{\frac{2}{3}} | E_1 = 30 \text{ eV} >$$

(C)
$$\frac{1}{2} | E_0 = 10 \text{ eV} > -\frac{\sqrt{3}}{4} | E_1 = 30 \text{ eV} >$$

(D)
$$\frac{1}{\sqrt{2}} | E_0 = 10 \text{ eV} > -\frac{1}{\sqrt{2}} | E_1 = 30 \text{ eV} >$$

- 21. Viscosity and surface tension are:
 - (A) Both intensive variables
 - (B) Both extensive variables
 - (C) Intensive and extensive variables respectively
 - (D) Extensive and intensive variables respectively
- 22. A capacitor of capacitance C farads is charged from a battery of emf V volts. Out of the work done by the battery an amount $\frac{1}{2}$ CV² is stored in the capacitor and the rest is released as heat. The released heat is:
 - (A) Zero
 - (B) CV²
 - (C) $\frac{\text{CV}^2}{8}$
 - (D) $\frac{\text{CV}^2}{2}$

23. van der Waals equation for one mole of gas is $\left(p + \frac{a}{V^2}\right)(V - b) = RT$. The equation for n moles would be :

(A)
$$\left(p + \frac{an}{V^2}\right)(V - nb) = nRT$$

(B)
$$\left(p + \frac{a}{V^2}\right)(V - b) = nRT$$

(C)
$$\left(p + \frac{an^2}{V^2}\right)(V - nb) = nRT$$

(D)
$$\left(p + \frac{an}{V^2}\right)(V - b) = nRT$$

24. The entropy of black-body radiation is given by S = $\frac{4}{3}\sigma V^{1/4}U^{3/4}$ where σ is a constant V is the volume and U is internal energy of the system. The temperature of the radiation is:

(A)
$$T = \frac{U^{1/4}}{\sigma V^{1/4}}$$

(B)
$$T = \frac{U^{1/4}}{\sigma}$$

(C)
$$T = \frac{1}{\sigma^4} \left(\frac{U}{V} \right)$$

(D)
$$T = \sigma \left(\frac{V}{U}\right)^{1/4}$$

- 25. A system consists of two identical particles. Each particle can occupy only two energy levels. E_1 = ϵ and E_2 = 2ϵ . If the particles satisfy Boltzmann statistics, the partition functions would be $\left(\beta = \frac{1}{k_{\rm B}T}\right)$:
 - (A) $z = e^{-3\varepsilon\beta}$
 - (B) $z = \frac{1}{2} (e^{-\beta \varepsilon} + e^{-2\beta \varepsilon})^2$
 - (C) $z = e^{-2\beta\varepsilon} + e^{-3\beta\varepsilon} + e^{-4\beta\varepsilon}$
 - (D) $z = 2(e^{-\beta \varepsilon} + e^{-2\beta \varepsilon})$

- 26. Crystaline sodium has 2 conduction electrons per unit cell with lattice constant (cube edge) 4.28 Å. In the free-electron model the Fermi temperature is ($h=6.62\times10^{-27}$ ergs, $c=3\times10^{10}$ cm/s, $m_e=9.1\times10^{-27}$ gm) :
 - (A) $T_F = 380 \text{ K}$
 - (B) $T_F = 3800 \text{ K}$
 - (C) $T_F = 38000 \text{ K}$
 - (D) $T_F = 38 \text{ K}$

which 4 particles can be distributed

in 7 energy levels if (i) they are

distinguishable and (ii) if they are

indistinguishable bosons respectively

is:

- (A) (i) $\frac{7!}{4!}$ and (ii) $\frac{7!}{4!3!}$
- (B) (i) 4⁷ and (ii) 210
- (C) (i) 7 ! 4 ! and (ii) $\frac{7 !}{4 ! 3 !}$
- (D) (i) 7⁴ and (ii) 210

28. One block of certain metal is at temperature T₁ and a second identical block is at a temperature T₂. These blocks are brought in contact and the system is thermally isolated from the surroundings. Assume that the heat capacity at constant volume C of each block is independent of temperature T. The increase in the entropy of the universe, when the system comes to an equilibrium is:

- $(A) \quad Cln \left[\frac{T_1T_2}{|T_2 T_1|} \right]$
- $(B) \quad C ln \left\lceil \frac{(T_1 + T_2)}{2T_1T_2} \right\rceil$
- (C) $C \ln \left[\frac{(T_1 + T_2)^2}{4T_1T_2} \right]$
- $(D) \quad C \ln \left[\frac{2T_1T_2}{T_1+T_2} \right]$

- 29. An ideal monoatomic gas at temperature 300 K is adiabatically decompressed so that the final volume is 8 times the original. The final temperature is:
 - (A) 150 K
 - (B) 37.5 K
 - (C) 2400 K
 - (D) 75 K
- 30. For one mole the van der Waals equation is

$$\left(p + \frac{a}{V^2}\right)(V - b) = RT$$

At the critical point the pressure is:

- (A) $P_c = \frac{a}{27b^2}$
- (B) $P_c = \frac{a}{27b}$
- (C) $P_c = \frac{a}{b}$
- (D) $P_c = \frac{a}{3b}$

- 31. To measure the temperature below the liquid Nitrogen temperature, we need to use :
 - (A) Thermocouple
 - (B) Semiconductor diode
 - (C) Transistor
 - (D) Thermister
- 32. In an experiment, the acceleration due to gravity is determined by measuring the time period of a simple pendulum. If there is an error of 1% in the measurement of time period, the error in the value of g is:
 - (A) 2%
 - (B) 1%
 - (C) 0.5%
 - (D) no error

- 33. A laser beam of intensity 50 W/cm² falls on a perfectly reflecting plane mirror for an hour. The area of the mirror is 5 cm². The average force acting on the mirror is few:
 - (A) Newtons
 - (B) Milli Newtons
 - (C) Micro Newtons
 - (D) Nano Newtons
- 34. When the movable mirror of

 Michelson interferometer is shifted
 through 0.0589 mm a shift of 200
 fringes is observed? The wavelength
 of light used in Å is:
 - (A) 5885
 - (B) 5890
 - (C) 5895
 - (D) 6000

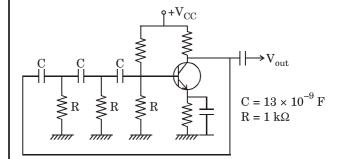
- 35. Photomultiplier can detect a feeble optical signal because of :
 - (A) The shape of its photocathode
 - (B) Multiplication of the output pulse
 - (C) Multiplication of secondary electrons
 - (D) Multiplication of photons
- 36. Which of the following gauges can measure the pressure in the range of 10^{-10} to 10^{-3} Torr ?
 - (A) McLeod gauge
 - (B) Pirani gauge
 - (C) Penning gauge
 - (D) Ionization gauge

- 37. A 10 stage photomultiplier tube has a stage gain of 4 secondary electrons. The overall amplification of the tube is:
 - (A) 10^3
 - (B) 10^4
 - (C) 10
 - (D) 10^6
- 38. In oil rotary pump for low vacuum, the oil primarily serves :
 - (A) As a lubricant
 - (B) To isolate rotating and stationary members of the group
 - (C) To discharge the exhaust against atmospheric pressure
 - (D) To prevent air from leaking into the pump side

- 39. For a typical laboratory sizes and specification which of the following has better resolving power?
 - (A) Prism spectrometer
 - (B) Grating spectrometer
 - (C) Fabry-Perrot etalon
 - (D) Constant deviation spectrometer
- 40. In which of the following wavelength region, the sources are comparatively weak and detectors insensitive requiring Fourier Transform methods:
 - (A) UV
 - (B) VISIBLE
 - (C) Infrared
 - (D) X-rays

- 41. A silicon diode dissipates 5 W of power when the dc current of 2 Amp flows through it. The bulk resistance of the diode is :
 - (A) 0.6Ω
 - (B) 0.9Ω
 - (C) 1.2 Ω
 - (D) 2.5Ω
- 42. For fabrication of light emitting diodes, the commonly used semi-conductor materials are :
 - (A) Pure crystals of silicon and germanium
 - (B) Thin waters of SiC and GaN
 - (C) $GaAs_{1-y}$ Py and GaP by deposition
 - (D) ZnSe, CdS and ZnTe in powder

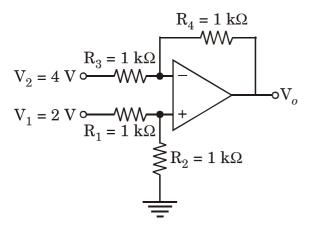
43. The frequency of the following phase shift oscillator:



is nearly equal to:

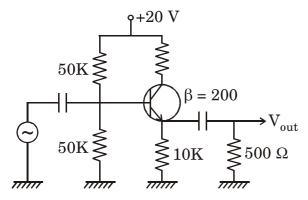
- (A) 2 kHz
- (B) 5 kHz
- (C) 8 kHz
- (D) 10 kHz
- 44. In a power supply circuit, the a.c. voltage of 100-0-100 Volts r.m.s. is applied to diodes of the full wave rectifier circuit. The output of the diodes is connected to a load of $5~\mathrm{k}\Omega$. The D.C. current through the load resistance of $5~\mathrm{k}\Omega$ is nearly :
 - (A) 15 mA
 - (B) 18 mA
 - (C) 21 mA
 - (D) 25 mA

45. The output voltage (V_o) of the following Op-amp circuit is :



- (A) + 2
- (B) 2
- (C) + 4
- (D) 4

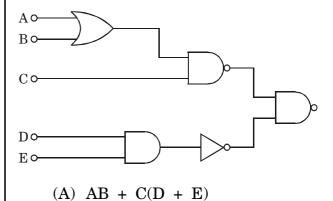
46. The voltage gain for the following amplifier circuit



is nearly equal to:

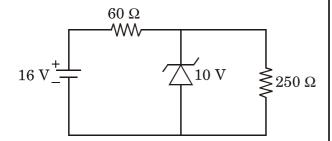
- (A) 0.5
- (B) 1.0
- (C) 1.5
- (D) 2.0

- 47. Negative feedback for an operational amplifier leads to :
 - (A) Increase the input and output impedance
 - (B) Increase the input impedance and the bandwidth
 - (C) Decrease the output impedance and bandwidth
 - (D) Does not affect impedance or bandwidth
- 48. The output of the following logic circuit is:



- (B) (A + B)C + DE
- (C) (A + B)C + D + E
- (D) (AB + C).DE

49. In the following zener diode circuit



the current flowing through the zener diode is:

- (A) 40 mA
- (B) 60 mA
- (C) 80 mA
- (D) 100 mA
- 50. Among the following A to D converter, the slowest one is the :
 - (A) Parallel comparator type
 - (B) Successive approximation type
 - (C) Integrating type
 - (D) Counting type

- 51. Value of radius for fifth orbital of hydrogen is (first orbital radius is0.53 Å):
 - (A) 0.529 Å
 - (B) 0.26 Å
 - (C) 8.4 Å
 - (D) 13.25 Å
- 52. The S, L and J values that correspond to each of the following states $^{1}\mathrm{S}_{0},~^{3}\mathrm{P}_{2}$ are :
 - (A) S = 0, L = 0, J = 0 and S = 1, L = 1, J = 2
 - (B) S = 1, L = 0, J = 0 and S = 2, L = 1, J = 2
 - (C) S = 0, L = 1, J = 1 and S = 1, L = 0, J = 2
 - (D) S = 1, L = 1, J = 2 and S = 2, L = 0, J = 2

- 53. In many electron atoms which of the following statements is *not* correct?
 - (A) In heavier atoms LS coupling is dominant
 - (B) In lighter atoms *jj* coupling is dominant
 - (C) LS coupling occurs irrespective of atomic size
 - (D) Electrostatic forces couple the l_i vectors into single L vector and S_i into another vector S
- 54. A typical PR contour for vibration-rotational spectrum for CO molecule shows $\Delta \overline{v} = 55 \text{ cm}^{-1}$. The associated value of rotational constant B is (Given; Boltzmann const. $k = 1.38 \times 10^{-23}$ J/K, T = 300, $h = 6.6 \times 10^{-34}$ J-s):
 - (A) 1.8 cm^{-1}
 - (B) 1.6 cm^{-1}
 - (C) 2.0 cm^{-1}
 - (D) 1.4 cm^{-1}

- 55. Which of the following is *not* correct (for number of fundamental modes of vibration)?
 - (A) Non-linear molecule has 3N-6 modes
 - (B) Non-linear molecule has 3N-3 modes
 - (C) Linear molecule has 3N-5 modes
 - (D) Spherical top molecule has 3N-6 modes
- 56. Direct confirmation about the quantization of internal energy states of an atom was first obtained from:
 - (A) Stern-Gerlach experiments
 - (B) Compton scattering experiment
 - (C) Millicon oil drop experiment
 - (D) Frank-Hertz experiment

57. When excited with mercury line at 435.8 nm, Benzene shows first Raman shift at 606 cm⁻¹. What will be the Raman shift if excited by He-Ne Laser (632.8 nm).

(Given : $n = 6.6 \times 10^{-34} \text{ Js}$) :

- (A) 1200 cm^{-1}
- (B) 409 cm^{-1}
- (C) 803 cm^{-1}
- (D) 606 cm^{-1}
- 58. Nuclear Magnetic Resonance (NMR) spectrometer normally operates at :
 - (A) Radio frequency region
 - (B) Microwave frequency region
 - (C) Audio frequency region
 - (D) Ultraviolet frequency region

- 59. Which of the following identity is *not* correct as regards the hybridization of atomic orbitals to form MO :
 - (A) sp^2 -Trigonal BCl_3
 - (B) sp-linear CO_2
 - (C) sp^3 -square planar $PtCl_4^{2-}$
 - (D) sp^3 -Tetrahedral CH_4
- 60. Which of the both sequences represent an increasing order of orbital energy ?
 - (A) 2p, 3s, 3p, 3d & 3s, 3p, 3d, 4s
 - (B) 3s, 3p, 3d, 4s & 4s, 5s, 6s, 7s
 - (C) 3s, 3p, 4s, 3d & 5s, 3d, 4f, 4p
 - (D) 3p, 4s, 3d, 4p & 2p, 3s, 3p, 4s

61. The primitive translational vectors
of the body centered lattice are given
by

$$\overrightarrow{a} = \frac{a}{2}(\hat{i} + \hat{j} - \hat{k}), \overrightarrow{b} = \frac{a}{2}(-\hat{i} + \hat{j} + \hat{k})$$

$$\stackrel{\rightarrow}{c} = \frac{a}{2}(\hat{i} - \hat{j} + \hat{k}),$$

where a is the side of the conventional unit cube and \hat{i} , \hat{j} , \hat{k} are orthogonal unit vectors parallel to the cube edges. The volume of the reciprocal lattice of bcc cell is :

- (A) $\frac{1}{2}a^3$
- (B) $2(2\pi/a)^3$
- (C) $(\pi/a)^3$
- (D) $(2\pi/3a)^3$

- 62. In a simple cubic crystal of lattice spacing a=3 Å, a positive edge dislocation 1 mm long climbs down by 1 μ m. The number of vacancies created or lost in the crystal is :
 - (A) 1.10×10^{10}
 - (B) 5.00×10^{12}
 - (C) 5.00×10^{14}
 - (D) 8.00×10^{15}
- 63. The Debye temperature of diamond is 2230 K. The molar heat capacity of diamond at 10 K is :
 - $(R = 8.314 \text{ Jmol}^{-1}\text{K}^{-1})$
 - (A) $0.025 \text{ Jkmol}^{-1}\text{K}^{-1}$
 - (B) $0.175 \text{ Jkmol}^{-1}\text{K}^{-1}$
 - (C) $0.235 \text{ Jkmol}^{-1}\text{K}^{-1}$
 - (D) $0.350 \ Jkmol^{-1}K^{-1}$

- has an ionization potential energy

 5 eV and X atom has an electron

 affinity. The amount of energy

 required to transfer an electron from

 M to X when they are at a distance

 of 5 Å is:
 - (A) 0.50 eV
 - (B) -2.88 eV
 - (C) 1.88 eV
 - (D) -4.20 eV

65. A linear diatomic lattice of lattice constant a with masses M and m(M > m) are coupled by a force constant C. The dispersion relation is given by

$$\omega^2 = C \left(\frac{1}{M} + \frac{1}{m} \right)$$

$$\pm \left[C^2 \left(\frac{1}{M} + \frac{1}{m} \right)^2 - \frac{4C^2}{Mm} \sin^2 ka \right]^{1/2}$$

Which one of the following statements is *incorrect* ?

- (A) The atoms vibrating in transverse mode correspond to the optical branch
- (B) The maximum frequency of the acoustic branch depends on the mass of the lighter atom m
- (C) The dispersion of frequency in the optical branch is smaller than that in the acoustic branch
- (D) No normal modes exist in the acoustic branch for any frequency greater than the maximum frequency at $k = \pi/a$

66. If the interatomic potential energy function can be expressed as

$$U(R) = - \frac{A}{R^6} + \frac{B}{R^{12}},$$

where A and B are constants, the atomic spacing \mathbf{R}_0 for which the potential energy is a minimum is given by :

- (A) A/4B
- (B) $(2B/A)^{1/6}$
- (C) $A^2/4B$
- (D) $4B^2/A$
- 67. For an ideal Fermi gas in threedimensions, the electron velocity $v_{\rm F}$ at the Fermi surface is related to electron concentration n as:
 - (A) $v_{\rm F} \propto n^{2/3}$
 - (B) $v_{\rm F} \propto n$
 - (C) $v_{\rm F} \propto n^{1/2}$
 - (D) $v_{\rm F} \propto n^{1/3}$

- 68. A phosphorous doped silicon semiconductor (doping density : 10^{17} /cm³) is heated from 100°C to 200°C. Which one of the following statements is *correct* ?
 - (A) Position of Fermi level moves towards conduction band
 - (B) Position of dopant level moves towards conduction band
 - (C) Position of Fermi level moves towards middle of the energy gap
 - (D) Position of dopant level moves towards the middle of the energy gap
- 69. For a rare earth ion the ground state energy level is characterized by the term value ${}^4I_{9/2}$. The number of 4f unpaired electrons in this ion is :
 - (A) 2
 - (B) 3
 - (C) 4
 - (D) 5

- 70. A flux quantum (fluxoid) is approximately equal to 2×10^{-7} gauss-cm². A type II superconductor is placed in a small magnetic field, which is then slowly increased till the field starts penetrating the superconductor. The strength of the field at this point is $(2/\pi) \times 10^5$ gauss. The penetration depth of this superconductor is:
 - (A) 10 Å
 - $(B)\ 100\ \mathring{A}$
 - (C) 1000 Å
 - (D) 1200 Å

- 71. The wavelength of 10 MeV proton is nearly equal to : $(1F = 10^{-15}$ meter)
 - (A) 7 F
 - (B) 9 F
 - (C) 11 F
 - (D) 13 F
- 72. The nuclear density of a ¹⁹⁷Au nucleus is nearly:

[Mass of 197 Au = 3.2707×10^{-25} kg,

$$r_0 = 1.2 \times 10^{-15} \text{ m}$$

- (A) $3.96 \times 10^{17} \text{ kg/m}^3$
- (B) $5.80 \times 10^{17} \text{ kg/m}^3$
- (C) $6.54 \times 10^{17} \text{ kg/m}^3$
- (D) $8.38 \times 10^{17} \text{ kg/m}^3$

- 73. Nuclear forces are:
 - (A) Spin dependent and have no non-central part
 - (B) Spin dependent and have a noncentral part
 - (C) Spin independent and have no non-central part
 - (D) Spin independent and have a non-central part
- 74. Given: Masses of $^{80}_{35}$ Br and $^{80}_{34}$ Se are respectively 79.918528 amu and 79.916520 amu. Use 1 amu = 931.5 MeV Nucleus $^{80}_{35}$ Br decays to $^{80}_{34}$ Se by emitting a positron. The end point energy of the emitted positron is nearly:
 - (A) 0.511 MeV
 - (B) 0.84 MeV
 - (C) 1.84 MeV
 - (D) 1.022 MeV

- 75. $_1\mathrm{H}^3$ nuclei undergoes beta decay at a rate of 1.27×10^{17} particles/hour and produce 21 calories of heat per hour in a medium. The average energy of the beta particle emitted
 - (A) 10.2 KeV

is:

- (B) 8.5 KeV
- (C) 6.4 KeV
- (D) 4.3 KeV

76. A gamma-ray of 3.43 MeV energy
undergoes pair production. The
electron and positron formed move
with equal kinetic energy in opposite
direction to each other. The kinetic

energy of the positron is nearly:

- (A) 0.511 MeV
- (B) 1.022 MeV
- (C) 1.20 MeV
- (D) 1.40 MeV

- 77. A gas filled G.M. counter cannot be used to measure energy of radiation because:
 - (A) The electrons and ions produced in the counter recombine and therefore energy information is lost.
 - (B) The window of the G.M. counter is thick and therefore a large fraction of the energy of radiation is lost while entering the counter.
 - (C) Only a fraction of the gas atoms of the G.M. counter are ionised and therefore the energy information is lost.
 - (D) All the atoms of the gas are ionised irrespective of the energy of incident radiation.The information about the energy of the radiation is lost.

78. The following nuclear reaction is induced by bombarding neutrons on the 13 C target.

$$^{13}\text{C} + n \rightarrow ^{10}\text{Be} + ^{4}\text{He}$$

If the R value of this reaction is -3.835 MeV, the minimum neutron energy required to induce the reaction is nearly:

- (A) 2.13 MeV
- (B) 4.13 MeV
- (C) 4.835 MeV
- (D) 5.835 MeV
- 79. The following particles

$$K^+, K^-, \pi^+, \pi^0, \pi^-, K^0$$

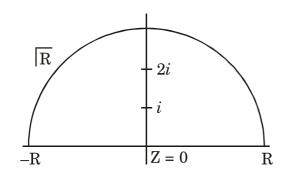
are broadly classified as:

- (A) Leptons
- (B) Quarks
- (C) Baryons
- (D) Mesons
- 80. Considering U, d, S Quarks, the quark content of proton and neutron are respectively:
 - (A) UUS and ddS
 - (B) UdS and dSS
 - (C) UUS and USS
 - (D) UUd and Udd

- 81. If $\overline{A} = x\hat{e}_x + y\hat{e}_y + z\hat{e}_j$, then $\nabla^2 \overline{A}$ will be:
 - (A) 1
 - (B) 3
 - (C) 0
 - (D) 3
- 82. If a vector field $\overline{F} = x\hat{i} + 2y\hat{j} + 3z\hat{k}$, then $\nabla \times (\nabla \times \overline{F})$ is :
 - (A) Zero
 - (B) \hat{j}
 - (C) $2\hat{j}$
 - (D) $3\hat{k}$
- 83. A gas molecule moves equal distances λ between successive collisions with equal probability in any direction. After a total of N such collisions, the mean square displacement of the molecule \bar{d}^2 will be:
 - (A) $N\lambda$
 - (B) $N\lambda^2$
 - (C) $N^2\lambda^2$
 - (D) $N^2\lambda$

- 84. At the origin, the function $f(z) = \sqrt{|xy|}$ is not analytic because :
 - (A) The Cauchy-Riemann (C-R) conditions are not satisfied at origin.
 - (B) $f'(0) \neq 0$ and the C-R conditions are satisfied at origin.
 - (C) f'(0) = 0 though the C-R conditions are satisfied at origin.
 - (D) f'(0) = 0 and the C-R conditions are not satisfied at origin.
- 85. I = $\int_{c} \frac{z^2 dz}{(z^2+1)(z^2+4)}$, in the *z*-plane.

Here c is a contour as shown:



then:

(A)
$$I = \pi/6$$

(B)
$$I = -\pi/3$$

(C)
$$I = 0$$

(D)
$$I = \pi/3$$

86. Consider a differential equation

$$\frac{d^2x}{dt^2} + 2\frac{dx}{dt} + x = 0$$

At time t = 0, it is given that x = 1 and $\frac{dx}{dt} = 0$. At t = 1, the value of

x is:

- (A) 1/e
- (B) 2/e
- (C) 1
- (D) 3/e
- 7. The solution of the differential equation $\frac{d^2y}{dt^2} y = 0$, subject to the boundary conditions y(0) = 1, $y(\infty) = 0$ is :
 - (A) $\cos t + \sin t$
 - (B) $\cosh t + \sinh t$
 - (C) $\cos t \sin t$
 - (D) $\cosh t \sinh t$

- 88. A matrix is said to be of rank zero if and only if:
 - (A) All the elements are non-zero, but the determinant is zero.
 - (B) It is equal to its own inverse.
 - (C) All its diagonal elements are zero.
 - (D) All its elements are zero.
- 89. The following Pauli spin matrices

$$\sigma_x = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$
 and $\sigma_y = \begin{bmatrix} 0 & -i \\ i & 0 \end{bmatrix}$

- (A) Commute
- (B) Anti-commute
- (C) Do not possess commutation relation
- (D) Are inverses of each other.

90. Fourier series for the function

$$f(\theta) = \begin{cases} +1 & 0 < \theta < \pi \\ -1 & \pi < \theta < 2\pi \end{cases}$$

there are:

- (A) Even cosine terms only
- (B) Both odd sine and cosine terms
- (C) Sine terms only
- (D) Odd sine terms only
- 91. A circular hoop of mass 'M' and radius 'a' rolls without slipping with constant angular speed ω along horizontal x-axis in the x-y plane. When the center of hoop is at a distance $d = \sqrt{2} a$ from the origin, the magnitude of total angular momentum of the hoop about the origin is:
 - (A) $Ma^2\omega$
 - (B) $\sqrt{2}$.M $a^2\omega$
 - (C) $2Ma^2\omega$
 - (D) $3Ma^2\omega$

- 92. A projectile is fired with initial velocity v_0 making an angle α with the horizontal axis. The range (R) of the projectile is proportional to, (Neglect the air resistance):
 - (A) v_0 and $\sin 2\alpha$
 - (B) v_0 and $\sin \alpha$
 - (C) v_0^2 and $\sin \alpha$
 - (D) v_0^2 and $\sin 2\alpha$
- 93. An artificial satellite revolves about the earth at height H (H << R, R = radius of earth). The orbital period, for which a man in the satellite will be in state of weightlessness is given as:
 - (A) $2\pi\sqrt{\frac{g}{R}}$
 - (B) $2\pi\sqrt{\frac{R}{g}}$
 - (C) $\frac{1}{2\pi}\sqrt{\frac{g}{R}}$
 - (D) $\frac{1}{2\pi}\sqrt{\frac{R}{g}}$

- 94. For repulsive inverse square force, the shape of the orbit is:
 - (A) Circular
 - (B) Parabolic
 - (C) Hyperbolic
 - (D) Elliptical
- 95. A unit charge q moving with initial velocity $(\overline{v} = v_x \hat{i})$ is subjected to external electric field $(\overline{E} = E_y \overline{j})$. The number of degrees of freedom is:
 - (A) 1
 - (B) 2
 - (C) Zero
 - (D) 3
- 96. For a Lagrangian $L(q, \dot{q}, \ddot{q}, t)$, the equation motion is of the form :

(A)
$$\frac{d^2}{dt^2} \left(\frac{\partial \mathbf{L}}{\partial \ddot{q}} \right) - \frac{\partial \mathbf{L}}{\partial q} = 0$$

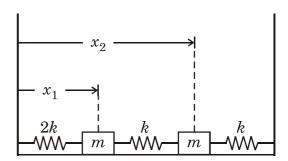
(B)
$$\frac{d^2}{dt^2} \left(\frac{\partial \mathbf{L}}{\partial \ddot{q}} \right) - \frac{d}{dt} \left(\frac{\partial \mathbf{L}}{\partial \dot{q}} \right) + \frac{\partial \mathbf{L}}{\partial q} = 0$$

(C)
$$\frac{d^2}{dt^2} \left(\frac{\partial \mathbf{L}}{\partial \ddot{q}} \right) + \frac{d}{dt} \left(\frac{\partial \mathbf{L}}{\partial \dot{q}} \right) + \frac{\partial \mathbf{L}}{\partial q} = 0$$

(D)
$$\frac{d^2}{dt^2} \left(\frac{\partial \mathbf{L}}{\partial \ddot{q}} \right) - \frac{d}{dt} \left(\frac{\partial \mathbf{L}}{\partial \dot{q}} \right) - \frac{\partial \mathbf{L}}{\partial q} = 0$$

- 97. The radius of gyration of a rigid body of mass M and moment of inertia I is:
 - $(A) (I/M)^2$
 - (B) $(M/I)^2$
 - (C) $(I/M)^{1/2}$
 - (D) $(M/I)^{1/2}$
- 98. The period of oscillation of the plane of Foucault's pendulum is :
 - $(\phi$ is the latitude)
 - (A) Directly proportional to the latitude (ϕ)
 - (B) Inversally proportional to $\sin\,\phi$
 - (C) Inversally proportional to $\cos\,\phi$
 - (D) Directly proportional to $\sin \phi$

99. Two masses are connected by springs (as shown in the figure). The potential energy matrix is:



- (A) $\begin{pmatrix} 2k & k \\ k & 2k \end{pmatrix}$
- (B) $\begin{pmatrix} 2k & -k \\ -k & 2k \end{pmatrix}$
- (C) $\begin{pmatrix} 3k & -k \\ -k & 3k \end{pmatrix}$
- (D) $\begin{pmatrix} 3k & k \\ k & 3k \end{pmatrix}$
- 100. A space ship is moving away from earth with velocity $0.4\ c$. It fires a rocket (away from earth) whose velocity is $0.5\ c$ with respect to the space ship. The velocity of the rocket as observed from the earth is :
 - (A) 0.75 c
 - (B) 0.80 c
 - (C) 0.60 c
 - (D) 0.90 c

ROUGH WORK

ROUGH WORK