		Test Bo	oklet Code a	&No.					
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	MATHEMATIC	CAL	SCIE	NCE	C		-	-	
Sigr	nature and Name of Invigilator		Seat No.						
1. (S	ignature)			(In f	igure	es as i	in Ad	mit C	ard)
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MA	AY - 30316			(To b	e fille	ed by	the C	andio	late)
Tim	e Allowed : 2½ Hours]			[]	Max	imur	n Ma	rks	150
Nun	ber of Pages in this Booklet : 48	Nu	umber of Q	uesti	ons i	n thi	s Boo	klet :	146
1. 2. 3.	 Instructions for the Candidates Write your Seat No. and OMR Sheet No. in the space provided on the top of this page. (a) This paper consists of One hundred forty six (146) multiple choice questions, each question carrying Two (2) marks. (b) Answer to first Four questions is compulsory. (c) Answer any 71 out of remaining 142 questions. In case any candidate answers more than 71 questions, only first 71 questions will be evaluated. (d) Below each question, four alternatives or responses are given. Only one of these alternatives is the 'CORRECT' answer to the question. At the commencement of examination, the question booklet will be given to the student. In the first 5 minutes, you are requested to open the booklet and compulsorily examine it as follows: (i) To have access to the Question Booklet, tear off the paper seal on the edge of this cover page. Do not accept a booklet without sticker-seal or open booklet. (ii) Tally the number of pages and number of questions in the booklet with the information printed on the cover page. Faulty booklets due to missing pages/ questions or questions repeated or not in serial order or any other discrepancy should not be accepted and correct booklet should be obtained from the invigilator within the period of 5 minutes. 	1. 2. 3.	परिक्षार्थांनी आपल तसेच आपणांस दि (a) या प्रश्नप दिलेले अ (b) पहिले (c) उरलेले च उत्तर देतो (d) खाली दि प्रश्नाचे क परीक्षा सुरू झाल्या मिनीटांमध्ये आपण पहाव्यात. (i) प्रश्नपत्रि सील नस (ii)	ा आसन व लेल्या उत्त त्रिकेत ए गहेत, प्रत्य चा. जर के , तर पहिल् दलेल्या प्र बहुपर्यायी वर विद्या बहुपर्यायी वर विद्या का उघडप लेली किं	कमांक या रिपत्रिकेत्त कृण क प्रश्ना श्नाचे च श्नाचे च उत्तरामधू र्थ्याला प्रश् नपत्रिका ग्यासाठी प्र वा सील	पृष्ठावरीः त्रा क्रमांक ला तर आवश् प्रश्नापे श्र्यी न केवळ न पत्रिका उघडून ख उघडलेर्ली	ल वरच्या त्याखार्ल यक आहेत को कोणते फ़रनांचे मूल किंवा उ एक ' बरोग दिली जा बालील बा केंवर लावत ो प्रश्नपत्रि	कोपऱ्यात लिहावा. बहुपय आहेत. 1. ही पेक्षा जास् तर दिलेल बा अवश्य बी अवश्य लेले सील का स्विव	लिहावा. र्ायी प्रश्न त प्रश्नांचे ईल. 1 आहेत. 1 ताम्यून उघडावे. जरू नये.
 4. 5. 6. 7. 8. 9. 10. 	 (iii) After this verification is over, the OMR Sheet Number should be entered on this Test Booklet. Each question has four alternative responses marked (A), (B), (C) and (D). You have to darken the circle as indicated below on the correct response against each item. Example : where (C) is the correct response. (A) (B) (D) Your responses to the items are to be indicated in the OMR Sheet given inside the Booklet only. If you mark at any place other than in the circle in the OMR Sheet, it will not be evaluated. Read instructions given inside carefully. Rough Work is to be done at the end of this booklet. If you write your Name, Seat Number, Phone Number or put any mark on any part of the OMR Sheet, except for the space allotted for the relevant entries, which may disclose your identity, or use abusive language or employ any other unfair means, you will render yourself liable to disqualification. You have to return original OMR Sheet to the invigilator at the end of the examination compulsorily and must not carry it with you outside the Examination Hall. You are, however, allowed to carry the Test Booklet and duplicate copy of OMR Sheet on conclusion of examination. 	4. 5. 6. 7. 8. 9.	(iii) वरीलप्रम ओ.एम.3 प्रत्येक प्रश्नासाठी आहेत. त्यातील य काळ्य/निळ करावा जर (C) हे या प्रश्नपत्रिकेतील इतर ठिकाणी लिहोत आत दिलेल्या सूच प्रश्नपत्रिकेच्या शेर जर आपण ओ.एम नाव, आसन क्रमां केलेली आढळून अ अवलंब केल्यास 1 परीक्षा संपल्यानंतर परत करणे आवश्य द्वितीय प्रत आपल्य	माणे सर्व आर. उत्तर' (A), (B), गेग्य उत्तर योग्य उत्तर योग्य उत्तर तेली उत्तर त तेली उत्तर त तेली उत्तर त तेली उत्तर दाडार्थ्या विद्यार्थ्यात क आहे. त् गाबरोबर न	े पडतात पत्रिकेचा (C) आगि ाचा रका र असेल र असेल प्रपासली ज तेल्या को तेल्या की तेल्या की प्रित्र किंव श्वया अस श्वयापी, प्रश्न	ठून पहि नंबर लिह नंबर लिह ग (D) अ ना खाली तर. जाणार नाही ाचाव्यात. न्या पानव् लेल्या ठि लेल्या ठि भय भाषेच अपात्र त .एम.आर नपत्रिका व नद्यार्थ्यांना	ल्यानंतरन शवा. शी चार f दर्शविल्ल करच कच्चे त. त. सरच कच्चे त. सरच कच्चे त. सरच काणा व्या परेल अ परवानगी	व प्रश्नप वेकल्प उ तरीक्त इत शी कोणत व्या इतर ¹ येईल. का पर्यवे आर. उत्तर आहे.	त्रिकेवर तरे दिल्ी उळकपणे र कोठेही ोही खूण रमार्गाचा स्रकांकडे पत्रिकेची
10. 11. 12.	Use of any calculator or log table, etc., is prohibited. There is no negative marking for incorrect answers.	11. 12.							

Mathematical Science Paper III

Time Allowed : 2¹/₂ Hours]

- Note : This paper consists of **One hundred forty six** (146) multiple choice questions, each question carrying **Two** (2) marks. Answer to first **Four** questions is compulsory. Answer any **71** out of remaining 142 questions. In case any candidate answers more than **71** questions, only first **71** questions will be evaluated.
- The optimal solution of the given 1 linear programming problem is : Max $z = 3x_1 + 5x_2$ Subject to constraints : $x_1 \leq 4$ $x_2 \leq 6$ $3x_1 + 2x_2 \le 18$ and $x_1, x_2 \ge 0$ (A) $x_1 = 2, x_2 = 6$ (B) $x_1 = 6, x_2 = 2$ (C) $x_1 = 0, x_2 = 6$ (D) $x_1 = 4, x_2 = 6$ 2. Suppose that the two constraints do not intersect in the first quadrant. Consider the following statements : (1) One of the constraint is redundant (2) The problem is infeasible (3) The solution is unbounded Then : (A) Only (1) is true (B) Both (1) and (2) are true
 - $(C) \quad Both \ (1) \ and \ (3) \ are \ true$
 - (D) Both (2) and (3) are true

- 3. For any primal problem and its dual, consider the following statements :
 - Primal will have an optimal solution if and only if dual does too
 - (2) Optimal value of the objective functions is same
 - (3) Both primal and dual cannot be infeasible
 - Then :
 - (A) Both (1) and (2) are correct
 - (B) Only (2) is correct
 - (C) Only (3) is correct
 - (D) Both (2) and (3) are correct

[Maximum Marks : 150

- In a mixed-integer programming problem, consider the following statements :
 - (1) All the decision variables require integer solutions
 - (2) Few of the decision variables require integer solutions
 - (3) Different objective functions aremixed together

Then :

(A)	Only (1) is correct
(B)	Only (2) is correct
(C)	Only (3) is correct
(D)	All are correct

- 5. Let K be the splitting field of the polynomial $x^3 + \pi x + 6$ over $F = Q(\pi)$ and K' be the splitting field of $x^3 + ex + 6$ over F' = Q(e). Then :
 - (A) $[K : F] \neq [K' : F']$
 - (B) [K : F] is infinite
 - (C) [K : F] = 6
 - (D) [K : F] is finite but [K' : F'] is infinite
- 6. Experience has shown that a certain lie detector will show a positive reading (indicates a lie) 10% of the time when a person is telling truth. Suppose that a random sample of 4 suspects is subjected to a lie detector test regarding a recent one-person crime. Then the probability of observing no positive reading if all suspects plead innocent and are telling the truth is :
 - (A) 0.4090(B) 0.7350
 - (C) 0.6561
 - (D) 0.5905

7. Let

 $F\,:\,X\,\rightarrow\,Y$

be a linear mapping from a normed linear space X to Y. Consider the following two statements.

(I) F is continuous at a point in X

(II) F is continuous at every point

in X

Then :

(A) (I) is always true

- (B) (II) is always true
- (C) (II) is true only when X is Banach
- (D) (II) is true only when (I) is true

8. In a triangle test a tester is presented with three fold samples, two of which are alike, and is asked to pick out the odd one by testing. If a tester has no well developed sense and can pick the odd one only, by chance, what is the probability that in five trials he will make four or more correct decisions ?

(A)
$$\frac{1}{243}$$

(B)

(C)

(D)

9. Let x be an element in a normed linear space X. Then there always exists a bounded linear functional f on X such that :
(A) f(x) = -1
(B) f(x) = 1

(C) f(x) = ||x||

5

(D) f(x) = ||x|| + 1

[P.T.O.

- 10. A study was conducted to investigate the effectiveness of a new drug. A group of patients was randomly divided into two groups. One group received the new drug; the other group received a placebo. The difference in mean subsequent surival (patients receiving drugspatients not receiving drugs) was found to be 1.04 years and a 95% confidence interval was found to be 1.04 ± 2.37 years. Based upon this information :
 - (A) We can conclude that the drug was effective because those receiving the drug lived, on average, 1.04 years longer
 - (B) We can conclude that the drug was ineffective because those receiving the drug lived, on average, 1.04 years less
 - (C) We can conclude that there is no evidence to conclude that the drug was effective because the 95% confidence interval covers zero
 - (D) We can arrive at no conclusion because we do not know the sample size nor the actual mean survival of each group

- 11. Let $\langle T_n \rangle$ be a sequence of continuous linear operators on a Banach space X to a normed linear space Y. Suppose that for each x in X the sequence $\langle T_n x \rangle$ converges to a value Tx. Then :
 - (A) T is bounded but need not be linear
 - $(B) \ T \ is \ bounded \ and \ linear$
 - (C) T is linear but need not be bounded
 - (D) T may not be bounded and may not be linear
- 12. A normal population distribution is needed for the following statistical procedure :
 - (A) Chi-squared test
 - (B) Variance estimation
 - (C) Student's *t*-test
 - (D) Kendall's rank coefficient

- 13. In a separable Hilbert space every orthonormal system is :
 - (A) infinite
 - (B) complete
 - (C) finite
 - (D) countable
- 14. In statistics :
 - (A) null hypothesis describes the probability that a relationship exists between two samples
 - (B) the mode is the measurement which lies exactly between each end of a range of values ranked in order
 - (C) skewed data invalidates further statistical analysis
 - (D) analytical statistics are the same as inferential statistics

- 15. Let X be locally path connected topological space. Then :
 - (A) every connected open set in X is path connected
 - (B) every connected set in X is path connected
 - (C) every connected closed set in Xis path connected
 - (D) every open set in X is path connected
- 16. Which of the following holds for Student's *t*-test ?
 - (A) It can be used to study the effect of an eye drop on intraocular pressure
 - (B) Its critical value is independent of the degrees of freedom
 - (C) It can be approximated by the z-test
 - (D) It is especially useful for multivariate analysis

17.	The one-point compactification of	19.	Which of the following spaces need
	${f R}^2$ is homeomorphic with :		not be normal ?
	(A) R ²		(A) Metrizable space
	(B) R		(B) Compact Hausdorff space
	(C) S ²		(C) Well ordered set with order
	(D) S ¹		topology
18.	Let X_1, X_2, \dots, X_n be a random		(D) Product of two normal spaces
	sample from U(0, θ). Let	20.	The pdf
	$X_{(n)} = \max\{X_1, \dots, X_n\}$		$f(x) = e^{- x - \theta } -\infty < x < \infty$
	then $X_{(n)}$ is :		has :
	(A) unbiased for θ		(A) MLR in x
	(B) unbiased and consistent for $\boldsymbol{\theta}$		(B) MLR in $-x$
	(C) consistent for θ		(C) MLR in x^2
	(D) UMVUE of θ		(D) MLR in $/x/$

- 21. Which of the following statements is not equivalent to any two of the remaining statements for a topological space X, where one point sets are closed ?
 - (A) X is completely regular
 - (B) X is metrizable
 - (C) X is homeomorphic to a subspace of a compact Hausdorff space
 - (D) X is homeomorphic to a subspace of a normal space
- 22. Suppose X and Y are independent r.v.s. each with a normal $\hat{\Psi}(\hat{\theta}) = \frac{10}{100}$ distribution, and
 - $E(X) = \theta, E(Y) = 3\theta,$

V(X) = V(Y) = 1.

Let be MLE of θ based on X and Y. Then :

(A) is biased and
(B) θ̂ is unbiased and
(C) θ̂ is biased and
(D) θ̂ is unbiased and

- 23. Let L be a lattice. Consider the following statements :
 - (1) Any two elements in L are comparable
 - (2) Any two elements in L are incomparable
 - (3) Every ideal of L is a maximal ideal
 - (4) Every ideal of L is a prime ideal

Then L is a chain iff :

- (A) Any of (1) and (4) holds
- (B) Both (1) and (3) hold
- (C) Any of (2) and (3) holds
- (D) Both (3) and (4) hold
- 24. A test ϕ is said to be similar if :
 - (A) $E_{HO}[\phi(X)] = \alpha$
 - $(B) \ E_{HO}[\phi(X)] \leq \alpha$
 - (C) $E_{HO}[\phi(X)] \ge \alpha$
 - (D) $E_{HO}[\phi(X)] > \alpha$

[P.T.O.

25. Consider the set N of natural numbers. Let ρ be a binary relation on N defined by $a \rho b$ iff a divides b.

Consider the following statements :

- (1) ρ is a partial ordering relation on N
- (2) N is a lattice under the relation ρ
- (3) N is a chain under the relation ρ
- (4) N is a complete lattice under the relation ρ

Then :

- (A) Only (1) is true
- (B) Both (2) and (3) are true
- (C) None of (1) to (4) is true
- (D) Both (1) and (2) are true

- 26. Significance of partial correlation coefficient is tested using :
 - (A) F-test
 - (B) *t*-test
 - (C) chi-square test
 - (D) z-test
- 27. Let R be a commutative ring. LetI(R) be the set of all ideals of R.Which of the following statementsis necessarily *true* ?
 - (A) I(R) is a distributive lattice
 - (B) I(R) is the empty set
 - (C) I(R) is a modular lattice
 - $(D) \ I(R) \ is \ not \ a \ lattice$

1	1 [P.T.O.
and inconsistent estimators of θ^2	(D) (1) holds
(D) is a sequence of biased	(C) (2) does not hold
	(B) (3) does not hold
consistent estimators of θ^2	(A) Either (2) or (3) holds
(C) is a sequence of biased	Then G is a tree iff :
inconsistent estimators of θ^2	(4) G contains a cycle
(B) is a sequence of unbiased	is a cut edge
	(3) G is connected and every edge
consistent estimators of θ^2	every pair of vertices in G
(A) $\left\{ \mathbf{T}_{n}^{2}\right\}$ is a sequence of unbiased	(2) There is a unique path between
consistent estimators of 0, then .	(1) G is acyclic
consistent estimators of 0 then i	following statements :
28. Let $\{T_n\}$ be a sequence of unbiased	29. Let G be a graph. Consider the

30	In a sample of size 100 there were	31.	Let R be the region defined by
00.	In a sample of size 100 there were		$\mathbf{R} : x \le a, y \le b.$
	50 smokers and 50 non-smokers. Out		Then the function
	of 50 smokers 30 suffered from		$f(x, y) = x \sin y + y \cos x$
	cancer and out of 50 non-smokers		satisfies the Lipschitz condition with
			Lipschitz constant K equal to :
	20 sufferred from cancer. The value		(A) <i>a</i>
	of chi-square statistic to test the		(B) <i>a</i> + 1
	association between smokers and		(C) <i>b</i>
			(D) $a + b$
	cancer is :	32.	If $x_1, x_2,, x_n$ is a sample from the
			Cauchy distribution with location
	(A) 4		parameter θ . \mathbf{Q}_i denotes <i>i</i> th quartile
			i = 1, 2, 3. Which of the following
	(B) 10		is a consistent estimator of θ .
			(A) Sample mean
	(C) 4.16		(B) Q ₂
	(D) 1		(C) Q ₁
			(D) Q ₃

33. The integral surface satisfying the partial differential equation 35. Let a string of uniform density ρ be xp + yq = zand passing through the circle stretched to a length *I* and fixed at $x^2 + y^2 + z^2 = 4$ x + y + z = 2points x = 0 and x = l and executes is : (A) x + y + z = 0a small transverse vibrations. Then (B) xy + yz + zx = 0(C) $x^2 + y^2 + z^2 = 0$ the total kinetic energy of the string (D) $\frac{x}{y} + \frac{y}{x} + \frac{z}{34} = 0$ 34. Multiple correlation between X₁ is given by : and (X_1, X_3) is : (A) $T = \frac{\rho}{2} \int_{0}^{T} \left[\left(\frac{\partial y}{\partial x} \right)^{2} + \left(\frac{\partial y}{\partial t} \right)^{2} \right] dx$ (A) $max(\rho_{12}, \rho_{13})$ (B) Correlation coefficient between (B) $T = \frac{\rho}{2} \int_{0}^{1} \left(\frac{\partial y}{\partial x}\right)^{2} dx$ X_1 and best linear predictor of ${\rm X}_1$ based on ${\rm X}_2$ and ${\rm X}_3$ (C) $T = \frac{\rho}{2} \int_{0}^{1} \left(\frac{\partial^2 y}{\partial x^2}\right) dx$ (C) Correlation coefficient between X_1 and $X_2 + X_3$ (D) Correlation coefficient between (D) $T = \frac{\rho}{2} \int_{0}^{1} \left(\frac{\partial y}{\partial t}\right)^{2} dx$ \mathbf{X}_1 and best predictor of \mathbf{X}_1 based on ${\rm X}_2$ and ${\rm X}_3$ 13 [P.T.O.

36.	Let z_1 and z_2 be independent standard normal variables. Let $Y_1 = Z_1 Z_2^2$. The correlation coefficient between Z_1 and Y_1 is :	38.	Suppose (X, Y) has Bivariate normal distribution with parameters $\mu_1 = \ , \ \mu_2 = \ ,$
	(A) 0		, ρ = .
	(B)		Then correlation coefficient between
	(C)		X – and Y –
	(D)		is :
37.	If $J_n(x)$ and $J_{-n}(x)$ be Bessel		(A)
	functions of first and second kinds. Consider the following relations :		(B)
	(1) $J_{-n}(x) = (-1)^n J_n(x)$		(C)
	(2) $J_n(-x) = (-1)^n J_n(x)$		(\mathbf{D})
	(3) $J_{-n}(x) = J_{n}(-x)$	20	Which of the following is a primitive
	Then :	39.	root of 23 ?
	(A) Only (3) is true		(A) 1
	(B) Only (1) and (2) are true		(B) 2
	(C) Only (2) and (3) are true		(C) 3
	(D) All (1), (2) and (3) are true		(D) 4

40. Let $(X_1, X_2, X_3)'$ follow three-variate Normal distribution with covariance matrix Σ , where :

> Let Y_i denote *i*th principal component of Σ , i = 1, 2, 3. Then correlation coefficient between (Y_1, Y_2) is :

$$\frac{\mathbf{a}}{\mathbf{g}}_{\Sigma} = \begin{bmatrix} 3.0 & 0.5 & 0.6 \\ 0.5 & 2.0 & 0.6 \\ 0.6 & 0.6^{\mathrm{C}} & 0 & 4.0 \end{bmatrix}$$

(D)

 (Λ)

41. For which of the following prime numbers p, both 2 and -1 are quadratic residues modulo p?
(A) 17
(B) 7
(C) 11
(D) 13

- 42. Given that we have collected pairs of observations on two variables X and Y, we would consider fitting a straight line with X as an explanatory variable if :
 - (A) the change in Y is a constant for each unit change in X
 - (B) The change in Y is an additive constant
 - (C) The change in Y is a fixed percent of Y
 - (D) The change in Y is exponential
- 43. Which of the following integers can be written as a sum of two squares ?
 (A) 720
 (B) 39
 - (C) 56

(D) 143

44.	For children, there is approximately	46. The yield of a grain, Y , appears
	a linear relationship between	to be linearly related to the amount
	"height" and "age". One child was	of fertilizer applied, X . An
	measured monthly. Her height was	experiment was conducted by
	75 cm at 3 years of age and 85 cm	fertilizer (0 to 10 kg/ha) to plots of
	when she was measured 18 months	measured. The following estimated
	later. A least square line was fit to	regression line was obtained. Y = a + bX
	her data. The slope of this line is	Which of the following is <i>not</i> true ?
	approximately :	(A) If no fertilizer was used, the
	(A) 0.55 cm/m	yield is estimated to be 4.85
	(B) 10 cm/m	(B) If fertilizer is applied at 10 ,
	(C) 25 cm/m	the estimated yield is 5.35
		(C) If the current level of fertilizer
	(D) 1.57 cm/m	is changed from 7.0 to 9.0
45.	is equal to :	the yield is estimated to
	(A) 216	increase by 0.20
	(R) 100	(D) To obtain an estimated yield
	(B) 100	of 5.2 , you need to apply
	(C) 108	
	(D) 156	7.0 of fertilizer

47. If L is a Lagrangian of a particle, the Lagrange's equations of motion are given by :

(A)

(B)
$$\frac{\partial \mathbf{L}}{\partial q_j} + \frac{d}{dt} \left(\frac{\partial \mathbf{L}}{\partial \dot{q}_j} \right) = \mathbf{0}$$

(C) $\frac{\partial \mathbf{L}}{\partial t} - \frac{d}{dt} \left(\mathbf{L} - \sum_j \dot{q}_j \frac{\partial \mathbf{L}}{\partial \dot{q}_j} \right) = \mathbf{0}$
 $\frac{\partial \mathbf{L}}{\partial t} = \frac{d}{dt} \left(\mathbf{L} - \sum_j \dot{q}_j \frac{\partial \mathbf{L}}{\partial \dot{q}_j} \right) = \mathbf{0}$

(D)
$$\frac{\partial \mathbf{L}}{\partial q_j} - \frac{d}{dt} \left[\mathbf{L} - \sum_j \dot{q}_j \frac{\partial \mathbf{L}}{\partial \dot{q}_j} \right] = 0$$

- $\dot{q}_j = \frac{\partial \mathcal{L}}{\partial q_j}$ 48. In single factor ANOVA, MSTr is the mean square for treatments, and MSE is the mean square error. Which of the following statements are *not* true ?
 - (A) MSE is a measure of within sample variation
 - (B) MSTr is a measure of between sample variation
 - (C) MSE is a measure of between sample variation
 - (D) The value of MSTr is affected by the status of (true or false)

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- 49. The Hamiltonian of a system represents total energy when it is :
 - (A) Non-conservative and scleronomic
 - (B) Conservative and rheonomic
 - (C) Conservative and scleronomic
 - (D) Conservative and kinetic energyis a homogeneous quadraticfunction of generalised velocities
- 50. In stratified sampling, the strata :
 - (A) are equal to each other in size
 - (B) are proportionate to the unitsin the target population
 - (C) are disproportionate to the unitsin the target population
 - (D) Can be proportionate or disproportionate to the units in the target population

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51. Let

	$\cos \theta$	$\sin \theta$	0
A =	$-\sin\theta$	$\cos \theta$	0
	0	0	1

be the matrix of orthogonal transformation, then its inverse is given by :

(A)

(B)

(C)

(D)

- 52. Cluster sampling is more efficient than simple random sampling if :
 - (A) Clusters are small and homogeneous
 - (B) Clusters are formed by grouping similar sampling units
 - (C) Clusters are internally heterogeneous
 - (D) Clusters are formed randomly
- 53. A particle is thrown horizontally from the top of a building of height *h* with initial velocity *u*, then :
 - (A) angular momentum of the particle is conserved
 - (B) linear momentum along horizontal direction is conserved
 - (C) linear momentum along vertical direction is conserved
 - (D) neither linear momentum nor angular momentum is conseved

- 54. Ratio estimator is more efficient than the sample mean if :
 - (A) The sample ratio is small
 - (B) The concomitant variable is strongly and positively correlated with the variable of interest
 - (C) The concomitant variable is independent of the variable of interest
- $\frac{x^2 y^2}{z} = 4$
- (D) The variable of interest is positive
- 55. Which of the following is *not* a surface ?
 - (A) $x^2 + y^2 = z^2$
 - (B) $x^2 + y^2 + z^2 = 1$
 - (C)

(D) $(x^2 + y^2)^2 + 3z^2 = 1$

- 56. Horvitz-Thompson estimator has a variance smaller than the sample mean because :
 - (A) Horvitz-Thompson estimator
 assumes probabilities
 proportional to the size of
 sampling units
 - (B) Horvitz-Thompson estimator
 assumes simple random
 sampling for selection of the
 sample
 - (C) Horvitz-Thompson estimator assigns unequal weights to sampling units
 - (D) Horvitz-Thompson estimator is similar to ratio estimator

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57. Let I be an open interval in the real line **R**. A curve $\alpha : I \to E^3$ in 3-dim. Euclidean space, defined by :

$$\alpha(s) = \left(\frac{4}{5}\cos(s), 1-\sin(s), -\frac{3}{5}\cos(s)\right)$$

represents :

- (A) a parabola
- (B) a hyperbola
- (C) an ellipse
- (D) a circle
- 58. Consider a symmetric BIBD with parameters v = b = 7, r = k = 3 and λ = 1. If C denotes the incidence matrix of the design, then det(C) is :
 - (A) 12
 - (B) 36
 - (C) 48
 - (D) 24

59. For a unit speed curve c : (x₁(s), x₂(s)) in E², the unit normal vector N is given by :
(A) (x'₂(s), x'₁(s))
(B) (x'₂(s), -x'₁(s))
(C) (-x'₂(s), x'₁(s))
(D) (-x'₂(s), -x'₁(s))

60. If

- [(1), ae, abc, bce, acd, cde, bd, abde] is the key block of a 2⁵ factorial experiment, then the confounded interactions are :
 - $(A) \ \textit{ace, bed, abcd}$
 - $(B) \ \textit{abc}, \ \textit{cde}, \ \textit{abcd}$
 - (C) ace, bcd, abde
 - (D) ade, bcd, abce

- 61. A curve α in $M \subset E^3$ is a geodesic of M if :
 - (A) its acceleration vector is always tangent to the surface M
 - (B) its acceleration vector is alwaysnormal to the surface M
 - (C) its acceleration vector is zero

(D) its acceleration vector and $\frac{\partial f}{\partial y} - \frac{d}{dx} \left(\frac{\partial f}{dy'} \right) = k$ velocity vector are orthogonal

> 62. The total number of Latin squares that can be obtained from a 4×4 square is :

(A) 16(B) 144(C) 24

(D) 64

63. The first integral of the Euler-Lagrange's differential equation of the functional

$$f = f(y, y')$$

is :

(A)

(B)
$$\frac{\partial^2 f}{\partial y^2} = k$$

(C)
$$f - y' \frac{\partial f}{\partial y'} = k$$

(D)
$$y' \frac{\partial f}{\partial y'} = k$$
,

where k arbitrary constant

- 64. The total number of factorial effects
 in a 2⁵ factorial experiment is :
 (A) 10
 (B) 32
 - (C) 31

(D) 5

65. Let y = y(x) be the extremal of the 66. Consider a time series functional $X_t = \sin(2\Pi \ U_t), t = 1, 2,...$ $I(y(x)) = \frac{1}{2} \int_{0}^{2} (y'')^{2} dx$ where U_{t} ~ uniform (0, 1). Then, which of the following statements and satisfy are *correct* ? y(0) = 1, y'(0) = 1,(*i*) $\{X_t\}$ is weakly stationary y(2) = 1, y'(2) = 0,(ii) {X_t} is strictly stationary (*iii*) $\{X_t\}$ is a periodic time series then : (iv) {X_t} has infinite variance (A) y = -**Codes** : (B) y = -+ x + 1(A) (i) and (ii)(B) (i) and (iii)(C) y =+ 1 (C) (ii) and (iv)(D) y =- X(D) (iii) and (iv)

68. Consider a stationary time series

 $\mathbf{Y}_t - \boldsymbol{\phi} \ \mathbf{Y}_{t-1} = \boldsymbol{\mu} + \mathbf{Z}_t - \boldsymbol{\theta} \ \mathbf{Z}_{t-1},$

where \mathbf{Z}_t is a white noise process

with mean zero and variance σ^2 ?

Which of the following statements

(A) $E(Y_t) = \mu$, $Var(Y_t) = \frac{\sigma^2}{(1-\phi^2)}$

 \mathbf{Y}_t given by

is true?

67. The condition(s) for the extremal of the integral

I(y(x)) =

where *y* is not prescribed at the end points is (are) :

(A)
$$\frac{\partial f}{\partial y} - \frac{d}{dx} \left(\frac{\partial f}{dy} \right) = 0$$

 $\begin{array}{c} \underbrace{\frac{\partial}{\partial f}}{\frac{\partial}{\partial y}} \underbrace{\frac{\partial}{\partial f}}{\frac{\partial}{\partial y}} \underbrace{\frac{\partial}{\partial f}}{\frac{\partial}{\partial y}} \underbrace{\frac{\partial}{\partial f}}{\frac{\partial}{\partial y}} = 0 \\ (C) \quad \frac{\partial}{\partial f}}{\frac{\partial}{\partial y}} - \frac{d}{dx} \left(\frac{\partial}{\partial f}}{\frac{\partial}{\partial y'}} \right) = 0 \quad \text{and} \\ \left(\frac{\partial}{\partial f'}}{\frac{\partial}{\partial y'}} \right)_{x=x_1} = 0 \\ (D) \quad \frac{\partial}{\partial f}}{\frac{\partial}{\partial y}} - \frac{d}{dx} \left(\frac{\partial}{\partial f'}}{\frac{\partial}{\partial y'}} \right) = 0, \\ \left(\frac{\partial}{\partial f'} \right)_{x=x_1} = 0, \\ \left(\frac{\partial}{\partial f'} \right)_{x=x_2} = 0 \\ (D) \quad E(Y_t) = , \\ \left(\frac{\partial}{\partial f'} \right)_{x=x_1} = 0, \\ \left(\frac{\partial}{\partial f'} \right)_{x=x_2} = 0 \\ (D) \quad E(Y_t) = , \\ (D) \quad E(Y_t)$

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69. The extremal of the functional

$$I = \int_{\theta_0}^{\theta} \sqrt{r^2 + r'^2} \ d\theta, \ r^1 = \frac{dr}{d\theta}$$

is :

(A) a catenary

- (B) a straight line
- (C) an arc of the great circle
- (D) a helix
- 70. Suppose Z_t 's are iid random variables with mean zero and variance one. Let

Which of the following statements are *correct* ?

- (*i*) X_t is an iid (0, 1) sequence
- (*ii*) X_t is a white noise (0, 1) sequence
- (*iii*) The autocorrelation function ρ_h of X_t vanishes for all *h*, except at h = 0
- (*iv*) X_t is a weak stationary process

Codes :

- (A) (i), (ii) and (iii)
- (B) (ii), (iii) and (iv)
- (C) (i), (iii) and (iv)
- (D) (i), (ii) and (iv)

71. The integral equation :

 $x(t) = \sin t + x(s) \, ds,$

is a :

- (A) linear integral equation ofVolterra type with convolutionkernel
- (B) linear integral equation of Fredholm type with convolution kernel
- (C) linear integral equation ofVolterra type with symmetric kernel
- (D) linear integral equation ofFredholm type with symmetric kernel

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72. Consider a random walk process

$$X_{t} = \mu + X_{t-1} + Z_{t}$$
where $Z_{t} \sim$ white noise $(0, \sigma^{2})$, then
which of the following statements is
true?
(A) (X_{t}) is a non-stationary process
(B) (X_{t}) is a stationary process
(C) $(X_{t} - t_{\mu})$ is a stationary process
(D) $\frac{\{X_{t} - t_{\mu}\}}{\sqrt{t}}$ is a stationary process
73. The solution of the integral
equation

$$\begin{bmatrix} \frac{3}{4} & \frac{1}{4} & 0\\ 1 & \frac{1}{2} & \frac{1}{4}\\ 0 & \frac{3}{4} & \frac{1}{4} \end{bmatrix} = \sec^{2}t - 1 + \int_{0}^{\pi/4} x(s) ds,$$

$$\begin{bmatrix} \frac{3}{4} & \frac{1}{4} & 0\\ 0 & \frac{3}{4} & \frac{1}{4} \end{bmatrix} = \sec^{2}t - 1 + \int_{0}^{\pi/4} x(s) ds,$$
(B) $x + x = 2$
(B)
(C) $x(0) + x = 1$
(D) $x + x = 0$
(D)
(D) $x + x = 0$
(D)

8π 66

P =

75.	The solution of integral equation	77.	The solution of the Volterra integral equation of first kind
			f(t) =
	is :		where $f(t)$ is known function with $f(0) = 0$ is :
	(A) <i>t</i>		(A) $f(t)$
	1		(B) $f'(t)$
	(B) $\frac{1}{t}$		(C) $f'(t) - f(t)e^t$
			(D) $f'(t) - f(t)$
	(C)	78.	If
			$\{X_n, n \ge 0\}$
	(D)		is a branching process with
			$\mathbf{E}(\mathbf{X}_1) = m, \ m < 1,$
76.	If		then
	$\{\mathbf{N}(t), t \ge 0\}$		
	is a Poisson process and		
	$\mathbf{X} = \mathbf{T}_n - \mathbf{T}_{n-1},$		
	where T_n and T_{n-1} are two		is :
	consecutive epochs at which occurrences of Poisson process take		(A) <i>mⁿ</i>
	place, then the distribution of		
	X is :		(B)
	(A) Poisson		
	(B) Binomial		(C) $m^n(m^n - 1)$
	(C) Geometric		m
	(D) Exponential		(D) $\overline{1-m}$

	2	7			[P.]	Г.О.
(D) {	1, 2, 4}		(D) Mode	e of the v	ital events	
(C) {	1, 2, 3}					,1100
(B) {	2, 3, 4		(C) Frequ	uencies of	the vital eve	ents
(A) {	1, 3, 4		(B) Media	an of the	vital events	ļ
Then	the closed set is :		(II) Micall			
and t	the four states are 1, 2, 3, 4.		(A) Mean	of the v	vital events	
	$\begin{bmatrix} 0.3 & 0.7 & 0 & 0 \\ 0.6 & 0.2 & 0.2 & 0 \end{bmatrix}$		generally	in the fo	ollowing form	1:
Р	$= \begin{bmatrix} 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$	82.	Vital st	atistics	are availa	ble
a four	r-state Markov chain is :		(D) $\mu E =$	Ξ Εμ		
(D) n 80 The t	10 root		$(\mathbf{C}) \Delta = \mathbf{V}$	v = 0		
(C) a	t least one root		(\mathbf{C})	5 57		
r	oots		(B) $\delta^2 E$ =	$= \nabla^2$		
(B) a	in undeterminable number of					
(A) (Dne root		(A) $\nabla =$	$\delta \mathrm{E}^{-1/2}$		
I(x) = the d	omain $[a, b]$.		Incorrect	:		
in [<i>a</i> ,	b] and $f(a) f(b) < 0$, then for 0, there is (and)			0	_	
79. If $f(x)$) is a real continuous function	81.	Which	of the	following	is

83. A rod is rotating in a plane. The following table gives the angle θ (radians) through which the rod has turned for various values of the time *t* second :

t	θ	
0	0	
0.2	0.12	
0.4	0.49	
0.6	1.12	
0.8	2.02	
1.0	3.20	
1.2	4.67	

The angular velocity of the rod,
when t = 0.6 second is
(A) 3.82 rad/sec
(B) 2.62 rad/sec
(C) 2.72 rad/sec

 $(D) \ \ 3.92 \ \ rad/sec$

- 84. Crude rate of natural increase of the population growth in the context of vital statistics is :
 - (A) The difference between the crude birth rate per thousand and the crude death rate per thousand
 - (B) Ratio of the crude birth rate per thousand and the crude death rate per thousand
 - (C) Crude birth rate per thousand multiplied by the crude death rate per thousand
 - (D) Crude birth rate per thousand, plus crude death rate per thousand

85. The largest eigen value of the matrix :

by p	ower method is
(A)	2.08
(B)	5.38
(C)	7.15
(D)	3.47

86. Given the following table for L_x the number of rabbits living at age x, complete the life table for rabbits :

x	\mathbf{L}_{x}
0	100
1	90
2	80
3	75
4	60
5	30
6	0

32:

(t-s)G(s-b)as x, y and z be three rabbits ofages 1, 2 and 3 years respectively, then what is the probability that, at least one of them will be alive for one year more :

(A)

(B)

(C)

(D)

87. If

 $L^{-1}{f(p)} = F(t)$ and $L^{-1}{g(p)} = G(t),$

then

$$\mathrm{L}^{-1}\{f(p)g(p)\}$$

is :

(A)

(B)
$$\int_{0}^{t} \mathbf{F}(s)\mathbf{G}(t+s) ds$$

(C)
$$\int_{0}^{t} \mathbf{F}(s) \mathbf{G}(s) ds$$

(D)
$$\int_{0}^{t} \mathbf{F}(s)\mathbf{G}(t-s) ds$$

- 88. The values in the following life table which are marked with question marks in the context of vital statistics are :
- Age $x: L_x$ d_x q_x p_x 20: 693435???21: 690673--(A) d_x = 6920, q_x = 0.99602, p_x = 0.00398.(B) d_x = 2762, q_x = 0.99602,
 - $p_{X} = 0.00398$ (C) $d_{X} = 6920, q_{X} = 0.00398,$ $p_{X} = 0.99602$
 - (D) $d_x = 2762, q_x = 0.00398,$ $p_x = 0.99602$

89. The Fourier sine transform of

$$\frac{1}{e^{\pi t} - e^{-\pi t}}$$

(A)
$$\left[\frac{e^{-p}+1}{e^{p}+1}\right] \cdot \frac{1}{2\sqrt{2\pi}}$$

(B)

is :

(C)

(D)

- 90. Two components each with reliability $\frac{1}{2}$ are arranged to form a series system with reliability $R_S(t)$, and then to form a parallel system with reliability $R_P(t)$. Then the difference $R_P(t) - R_S(t)$ is :
 - (A)

(B)

(C)

(D)

- For what value of *r*, the component 91. The Fourier transform of the second 94. reliability, a 2-out-of-3 system will derivative of u(x, t) is : have reliability $\frac{1}{2}$? (A) *p* (p, t)(B) p^2 (A) (p, t)(p, t)(C) –*p* (B) (D) $-p^2$ (p, t)92. Which of the following relations is (**C**) true ? (D) (A) MTSF = 95. Let be the vector field given by (B) MTSF = exp $\left\{-\int_{0}^{\infty} R(t) dt\right\}$ $(x, y) = y + (x^2 + y)$ Then the line integral of A(0, 0) to B(1, 1) along the line AB is : (C) MTSF = exp $\left\{ \int_{0}^{\infty} r(t) dt \right\}$ $\mathbf{R}(\mathbf{x}) d\mathbf{x}$ (A) (B) (D) MTSF = $\int_{a}^{\infty} R(x) dx$ (C) 2 (D) 1 93. The solution of the integral 96. A double sampling plan has the following parameters : N = 2000, equation : $n_1 = 40, C_1 = 2, n_2 = 80$ and $x(t) = e^{-t} - 2\int_{0}^{t} \cos((t-s)x(s)ds)$ $C_2 = 4$. It is observed that the first sample contains 3 defectives, then in order that plan accepts the lot, the number of defectives in the by using Laplace transform is : (A) $x(t) = e^{-t^2}(1 + t)^2$ second sample should not exceed : (A) 1 (B) $x(t) = e^{-t}(1 + t)^2$ (B) 2 (C) $x(t) = e^{-t^2}(1 - t)^2$ (C) 3 (D) $x(t) = e^{-t}(1 - t)^2$ (D) Cannot be determined 31

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from

97. The value of the integral

where C is shown in the figure is :

,



- (A) $-4\pi i$
- (B) $4\pi i$
- (C) $2\pi i$
- $(D) \ zero$
- 98. If small orders and placed frequently rather than placing large orders infrequently, then total inventory cost gets :
 - (A) Reduced
 - (B) Increased
 - (C) Either reduced or increased
 - (D) Minimized

99. The value of the integral

$$\int_{\mathcal{C}} \frac{e^z}{\left(z+1\right)^3} \, dz$$

where C : |z| = 3 is : (A) $\pi i e$

- (B) $\frac{\pi i}{e}$
- (C)
- (D) $2\pi i e$
- 100. In the context of inventory models service level is defined as the probability of :
 - (A) Stocking during each order cycle
 - (B) Not stocking during each order cycle
 - (C) Stocking during lead time
 - (D) Not stocking during lead time
- 101. The value of the integral

where C is
$$|z - 1| = \frac{1}{2}$$
 is equal
to :
(A) $\pi i e$
(B) πi
(C) $-\pi i e$
(D) $i e$

- 102. At certain health care centre, patients arrive at a mean rate of 4 per hour and they are checked by doctor at a mean rate of 5 per hour. The centre feels that service times have some unspecified positive skewed unimodal two-tails distribution with a standard deviation of 0.05 hours. What is the average queue length and average waiting time of the patients spend in the health care centre ?
 - $\left(A\right)~2.5$ and 0.625 hours
 - $\left(B\right)~1.7$ and 0.425 hours
 - $\left(C\right)$ 1.7 and 0.625 hours
 - $\left(D\right) \ 2.5$ and $0.425 \ hours$
- 103. Which of the following is a set of positive measure ?
 - (A) The set of rational number in [0, 1]
 - (B) The set of numbers in [0, 1] not containing the digit 2 in their decimal expansion
 - $\left(C\right)$ The Cantor set
 - (D) The set of transcendental numbers in [0, 1]

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- 104. For a queueing system, which of the following statements is *correct* ?
 - (1) For a workable queueing systemit is necessary that the arrivalrate of customers per unit oftime should be grated than theservice rate
 - (2) Queues in series are those where input of a queue is derived from the output of another queue
 - (3) Circular queue are those wherea customer after being servedjoins back the queue again
 - (4) When the queueing systems are allowed to depend upon time and are controlled, then these system are known as dynamic control systems

Codes :

- (A) (1) and (2)
 (B) (1) and (3)
 (C) (1), (2) and (4)
 (D) (2) (2) (4)
- (D) (2), (3) and (4)

105. Which of the following is *false*?

- (A) If f is absolutely continuous on
 - [0, 1] then *f* is bounded variation on [0, 1]
- (B) If f is non-negative and absolutely continuous on [0, 1], then so is f
- (C) If f is non-negative and absolutely continuous on [0, 1], then is absolutely continuous on [0, 1]
 (D) If f is convex on (0, 1) then f
 - is absolutely continuous on every closed subinterval [*a*, *b*]

 \subset (0, 1)

- 106. Which of the following statements are *correct* in decision analysis ?
 - (1) Organisational decisions are the decisions taken by the executives in their official capacity
 - (2) Tactical decisions are the decisions taken by the executives in their individual capacity
 - (3) Strategic decisions which have far reaching effect on the future course of action
 - (4) Major decisions are the decisions which involve large sum of money and require prior sanction

Codes :

- (A) (1), (2) and (3)
 (B) (2), (3) and (4)
 (C) (1), (3) and (4)
- (D) (1), (2) and (4)

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107. Let $\{f_n\}_{n \ge 1}$ be negative meas Then :	a sequence of non- urable functions.	 109. Which of the following is <i>false</i>? (A) If μ and ν are signed measures and ν is absolutely continuous w.r.t. μ (i.e. ν μ), then ν is absolutely continuous w.r.t. μ
	2	(B) If μ is a measure, exists
	$\inf f_n \ dx$	and $v(E) = $, then v is
(B) lim inf	\leq inf $f_n dx$	 absolutely continuous w.r.t. μ (C) If [[X, S, μ]] is a σ-finite measure space and v is any σ-finite measure on S, then there is a finite-valued non-negative measurable function for X such
(C) lim inf	=	that for each $E \in S$, $v(E) =$
(D) lim sup	$\inf f_n \ dx$	(D) If [[X, S, μ]] is a σ -finite measure space and ν is a σ -finite signed measure such that $\nu = \mu$, then there exists a finite-valued measurable function <i>f</i> on X such
	$\sup f_n dx$	that for each $E\inS,\nu(E)$ =
108. When a positive parts, the maxim product is :	<i>q</i> is divided into five num value of their	110. Using dynamic programming, the maximum value of $3x_1 + 5x_2$ subject to
(A)		$x_1 \leq 4$ $x_2 \leq 6$ $3x_1 + 2x_2 \leq 18$ and
(B) 5q		$\begin{array}{ccc} & & 1 \\ & & x_1, & x_2 \geq 0 \\ & & & 1 \end{pmatrix}$
(C) $(5q)^5$		(A) 46 (B) 63
(D)		(C) 36 (D) 32

E55

111. Which of the following is a compact subset of \mathbf{R}^2 ?

(A) The x-axis

- (B) The set of all points in \mathbf{R}^2 having integer coordinates
- (C) The set $\{(x, y) | |x| + |y| \le 1\}$
- (D) $\{(x, y) \mid y^2 = x\}$
- 112. A set of values (x_0, y_0) , (x_1, y_1) , (x_2, y_2) , ..., (x_n, y_n) satisfying the relation y = f(x) is given, where the explicit nature of f(x) is not known. It is required to find a function $\phi(x)$ such that f(x) and $\phi(x)$ agree on the set of tabulated points. The method used for this is called :
 - (A) extrapolation
 - (B) polynomial extrapolation
 - (C) interpolation
 - (D) polynomial interpolation

113. Consider the following integrals :

(2)
$$\int_{0}^{\infty} \frac{\sin x \, dx}{\left(1+x\right)^2}$$

Here [x] is the integral part of x. Then :

- (A) Both (1) and (2) converge absolutely
- (B) None of (1) and (2) converges absolutely
- (C) only (1) converges absolutely
- (D) only (2) converges absolutely

114. The certain corresponding values of

x and $\log_{10} x$ are :

x	$\log_{10} x$
300	2.4771
304	2.4829
305	2.4843
307	2.4871

The value of $\log_{10} 301$ by Aitken's method (interpolation by iteration) is :

- (A) 3.4785
- (B) 3.4786
- (C) 2.4785
- (D) 2.4786
- 115. The Taylor series for $(1 \cos x)e^{x^2}$ about 0:
 - (A) contains only even powers of x
 - (B) contains only odd powers of x
 - (C) contains even as well as odd powers of x
 - (D) contains only powers of x of the type x^{k^2} , $k = 1, 2, \dots$.

116. The value of

$$\int_{0}^{1} \frac{1}{1+x} dx$$

correct to three decimal places by the trapezoidal rule, with h = 0.5and :

	x	$\frac{1}{1+x} = y$
	0.0	1.000
	0.5	0.6667
	1.0	0.5000
(A)	0.708	
(B)	0.608	
(C)	0.806	
(D)	0.807	

117. For which of the following functions the equation f(x, y) = 0 can be solved for y in terms of x in a neighbourhood of (0, 0)? (A) $f(x, y) = (x - 1)^2 + y^2 - 1$ (B) $f(x, y) = x^3 - y^2$ (C) $f(x, y) = x - y^2 \cos y$

(D)
$$f(x, y) = x \sin y + y \cos x$$

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118. The solution to the following	120. Which of the following terms refers
simulataneous equations is :	to a statistical method that can
0.0002x + 0.3003y = 0.1002	be used to statistically equate
2.0000x + 3.0000v = 2.0000	groups on a pretest or some other
	variable ?
(A) $x = 0.5000; y = 0.4444$	(A) Experimental control
(B) $x = 0.4444; y = 0.5000$	(B) Interaction effect
(C) $x = 0.3333; y = 0.5000$	(C) Treatment contrasts
(D) $x = 0.5000; y = 0.3333$	$(\mathbf{D}) \mathbf{A} = 1 \mathbf{a} = 1 \mathbf{a} = 1$
119 Let	(D) Analysis of covariance
	121. The value of the integral
$f\colon {f C} o {f R}$	
be a function defined by	
f(z) = z	where
for every $z \in \mathbb{C}$.	C : z = 3,
Then :	is equal to :
Then .	
(A) $f(0) = 0$	(A) 0
(B) $f(z)$ exists only at $z = 0$	(B) <i>-πi</i>
(C) $f(z) = 0$ for $z \neq 0$	(C) π <i>i</i>
(D) $f(z)$ does not exit at any $z \in \mathbb{C}$	(D) 2π <i>i</i>

- 122. When interpreting a correlation coefficient expressing the relationship between two variables, it is very important to avoid
 - (A) Checking the strength of relationship
 - (B) Expressing a relationship with a correlation coefficient
 - (C) Checking the direction of the relationship
 - (D) Jumping to the conclusion of causality
- 123. The number of non-isomorphic abelian groups of order *pqr*, where*p*, *q*, *r* are distinct primes is :
 - (A) 1
 - (B) 2
 - (C) 3
 - (D) 4

- - (A) Populations, statistics, samples
 - (B) Populations, parameters, samples
 - (C) Parameters, statistics, populations
 - (D) Parameters, populations, samples
- 125. Let F be a field with p^n elements, p is prime. Consider the following statements :
 - (1) (F, +) $\cong z_p \oplus \dots \oplus z_p$ (*n* copies of z_p)
 - (2) $\mathbf{F}^* \cong \mathbf{Z}_{p^n-1}$
 - (3) $F \{0\}$ is a cyclic group under multiplication.

Then which of the following is *true* ?

- (A) Only (1) is true
- (B) Only (2) is true
- (C) Only (3) is true
- (D) All the statements are true

126. The following table represents the relative frequency of accidents per day in a city :

Accidents	Relative	
	Frequency	
0	0.55	
1	0.20	
2	0.10	
3	0.15	
4 or more	0	

Which of the following are true ?

- (I) The mean and modal number of accidents are equal
- (II) The mean and median number of accidents are equal
- (III)The median and modal number of accidents are equal
- (A) (I), (II) and (III)
- (B) (I) only
- (C) (II) only
- $(D) \ (III) \ only$

- 127. Let T_1 and T_2 be linear operators on a finite dimensional vector space V over a field F. Suppose T_1 and T_2 are similar. Consider the following statements :
 - (1) T_1^2 and T_2^2 are similar
 - (2) are similar (if inverse exist)
 - (3) T_1T_2 and T_2T_1 are similar, given that at least one of T_1 and T_2 is invertible
 - (4) $T_1 + T_2$ and $T_1 T_2$ are similar
 - Then :
 - (A) Only (1) is true
 - (B) Only (4) is true
 - (C) None of (1) to (4) is true
 - (D) Each of (1), (2) and (3) are true

128. Let X be a uniform (0, 1) and Y be a Bernoulli random variable, independent of each other. Define :	129. For a matrix A, the characteristic polynomial is $\Delta(\lambda) = (\lambda - 2)^4$ $(\lambda - 3)^2$ and the minimal polynomial is $m(\lambda) = (\lambda - 2)^2 (\lambda - 3)^2$. Then a Jordan canonical form of A is :
Which of the following statements	(A)
are <i>correct</i> ?	
(<i>i</i>) The cumulative distribution function of z is	
$F_z(z) = 0.5 I_{(0 \le z \le 1)} + 0.5 I_{\{z = 1\}}$	(B)
$\begin{bmatrix} 1 \\ 2 \end{bmatrix} = \begin{bmatrix} 11017 & 00 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 $	
0 $0^{[X_{2}]} \overline{0}^{Y_{1}} \overline{10}^{1} 0 0$ OLebesgue-Stieltje's measure	
0 0 00 22 0 00 Ogenerated by F _z	
$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}_{3}^{A} \text{ dominating measure is } \lambda + \nu, \\ \text{where } \lambda \text{ is the Lebesgue}$	(C)
measure and v is the counting	
measure on {1}	
Codes :	
(A) (<i>i</i>) and (<i>ii</i>)	
(B) (<i>ii</i>), (<i>iii</i>) and (<i>iv</i>)	(D)
(C) (<i>ii</i>) and (<i>iii</i>)	
(D) (<i>i</i>), (<i>iii</i>) and (<i>iv</i>)	

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130. Let X ₂ , X ₃ , be random-variables	132. Let $\{X_k\}$ be a sequence of
such that for $\alpha > 0$	independent random variables
	with :
$P[X_n = 1] = 1 - ,$	$D[\mathbf{V} = k] = -D[\mathbf{V} = k]$
	$\mathbf{I}[\mathbf{A}_k = \mathbf{A}] = \mathbf{I}[\mathbf{A}_k = -\mathbf{A}]$
$\mathbf{P}[\mathbf{X}_n = n] = , \ n \ge 2.$	$P[X_k = 0] = 1 - k^{-\lambda}, \lambda > 0$
Which of the following statements	
are <i>correct</i> ?	Let $S_n = \dots$. Which of the
(<i>i</i>) X _n 1	following statements are <i>correct</i> ?
(<i>ii</i>) X _n 1	(i) $E(X_k) = 0$, $= Var(S_n) \to \infty$
(iii) X ₂ 1	for all λ
$(iv) \mathbf{X} = 1$	(<i>ii</i>) $E(X_k) = 0$, $Var(S_n) \rightarrow \infty$ for
(1) Λ_n 1	$\lambda \leq 3$
Codes :	(iii) Central limit theorem
(A) (<i>i</i>), (<i>ii</i>) and (<i>iii</i>)	
(B) (<i>i</i>), (<i>ii</i>) and (<i>iv</i>)	\rightarrow N(0, 1) hold for 0 < λ \leq 1
(C) (<i>i</i>) and (<i>ii</i>)	(<i>iv</i>) Central limit theorem $\mathbf{F}\left(\frac{\mathbf{S}_n}{\mathbf{S}_n}\right)$
(D) (<i>i</i>), (<i>ii</i>), (<i>iii</i>) and (<i>iv</i>)	(\mathbf{N}) contrar mine dicorcia $\mathbf{I}(\mathbf{S}_n)$
131. Which of the following groups has	\rightarrow N(0, 1) hold for 0 < λ < 1
a subgroup which is not normal ?	Codes :
(A) Z ₂₀	(\mathbf{A}) (<i>i</i>) and (<i>iii</i>)
(B) $Z_3 \times Z_6$	
(\mathbf{C}) \mathbf{O} the group of quaternions	(B) (<i>ii</i>) and (<i>iii</i>)
with 8 elements	(C) (<i>i</i>) and (<i>iv</i>)
(D) S ₃	(D) (11) and $(1V)$

	133. Let X be a metric space. Consider	134. Let X_n be a sequence of random variables such that
	the following statements :	$P[X_n = 0] = 1 - \frac{1}{n^2},$
	(1) X is compact	$\mathbf{P}[\mathbf{X}_n = e^n] = \dots$
	(2) X has Bolzano-Weierstrass	Which of the following statements
	property	are <i>correct</i> ?
(3) X is sequencia (3) X is sequencia (4) X is complete Then which of the true ? (A) (4) \Leftrightarrow (1) (B) (3) \Leftrightarrow (4) (C) (2) \Leftrightarrow (4)	(3) X is sequencially compact	(<i>i</i>) X _n 0
	(4) X is complete	(<i>ii</i>) X _n 0
	Then which of the following is	$(iii) X_n = 0$
	true ?	$(iv) X_n = 0$
	(A) (4) \Leftrightarrow (1)	Codes :
	(B) (3) \Leftrightarrow (4)	(A) (<i>i</i>), (<i>iii</i>) and (<i>iv</i>) (D) ((), (<i>ii</i>), (<i>iii</i>), (<i>iii</i>)
	(C) (2) \Leftrightarrow (4)	(B) (1), (11) and (111) (C) (1) (11) and (111)
	(\mathbf{D}) $(1) \Leftrightarrow (2)$	(U) (1), (11) and (1V) (D) (11) (11) (11)
	$(\mathbf{D}) \ (1) \ \leftrightarrow \ (2)$	(D) (11), (111) and (1V)

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135.	Which of the following metric spacesis <i>not</i> separable ?(A) R with usual metric	137. Wh con (A) (B)	ich of the nplete ? The ope R ⁿ	e following spaces is <i>not</i> en interval (0, 1)
	(B) C [0, 1]	(C)	{0}	
	(C) R with discrete metric	(D)	$C(\mathbf{R})$	
	(D) The space I_2 of square	138. The hor blo	e number nes on a ck is dese	of adults (X) living in randomly selected city cribed by the following
	summable real sequences	pro	bability o	distribution :
136.	A coin is tossed three times. What		X	Prob.
	is the probability that it lands on		2	0.15
	is the probability that it lands on heads exactly one time ?		2 3	0.15 0.15
	is the probability that it lands on heads exactly one time ? (A) 0.125	Wh	2 3 4 at is the probabil	0.15 0.15 0.10 e standard deviation of ity distribution ?
	is the probability that it lands onheads exactly one time ?(A) 0.125(B) 0.275	Wh the (A)	2 3 4 at is the probabil 0.89	0.15 0.15 0.10 e standard deviation of lity distribution ?
	 is the probability that it lands on heads exactly one time ? (A) 0.125 (B) 0.275 (C) 0.375 	Wh the (A) (B) (C)	2 3 4 at is the probabil 0.89 0.79 0.62	0.15 0.15 0.10 e standard deviation of lity distribution ?

- 139. Which of the following is *not* a complete space ?
 - (A) C[a, b], $a, b \in \mathbf{R}$
 - (B) The space of continuous functions on [0, 1] taking positive values
 - (C) B(X), the space of bounded real valued functions on an infinite set X
 - (D) L_1 , the space of Lebesgue integrable functions on **R**
- 140. A crop insurance company establishes the following loss table based upon previous claims :

Percent loss	Prob.
0	0.90
25	0.05
50	0.02
100	?

If they write policy that pays a maximum of \$150/hectare, their expected loss in \$/hectare is approximately :

- (A) 5.2
- (B) 7.9
- (C) 4.5
- (D) 25.0

- 141. Suppose two permutations of a symmetric group have the same orders of their cyclic decompositions. Then they are always :
 - (A) identical
 - (B) Inverse of each other
 - (C) Conjugates of each other
 - (D) Commute with each other
- 142. The average length of stay in a hospital is useful for planning purposes. Suppose that the following is the distribution of the length of stay in a hospital after a minor operation :

Days	Prob.
2	0.05
3	0.20
4	0.40
5	0.20
6	?

The average length of stay is :

- (A) 0.15
- (B) 2.25
- (C) 4.20
- (D) 5.50

- 143. Let F be a proper subfield of the complex field C which is algebraically closed. Then :
 - (A) F is infinite dimensional over \mathbf{Q}
 - (B) F is finite dimensional over ${\boldsymbol R}$
 - (C) Characteristic of F is non-zero
 - (D) Such a field does not exist
- 144. Acme Toy company sells baseball cards in packages of 100. These types of players are represented in each package—rookies, veterans, and All-Stars. The company claims that 30% of the cards are rookies, 60% are veterans, and 10% are All-Stars. Cards from each group are rundomly assigned to packages.

Suppose you bought a package of cards and counted the players from each group. What method would you use to test Acme's claim that 30% of the production run are rookies; 60% veterans; and 10% All-Stars.

- (A) Chi-square goodness of fit test
- (B) Chi-square test for homogeneity
- (C) Chi-square test for independence
- (D) One sample *t*-test

- 145. Which of the following statements is *not* true ?
 - (A) Galois extension over a Galois extension is a Galois extension
 - (B) Separable extension over a separable extension is separable
 - (C) Algebraic extension over an algebraic extension is algebraic
 - (D) Inseparable extension over an inseparable extension is inseparable
- 146. Which of the following would be a reason to use a one-sample *t*-test instead of one-sample *z*-test ?
 - (*i*) The standard deviation of the population is unknown
 - (*ii*) The null hypothesis involves a continuous variable
 - (*iii*) The sample size is large (greater than 40)

Codes :

- (A) (i) only
- (B) (ii) only
- (C) (iii) only
- (D) (i) and (iii)

ROUGH WORK

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